

Principle of GNSS (GPS) Positioning

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Training Class

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1 Introduction

What is GNSS (GPS) , the main segments and development

Global Navigation Satellite System

GPS(USA) Global Positioning System

GLONASS(Russia) Global Navigation Satellite System

Galileo (Europe, China and India)

Compass Navigation Satellite System (China)

Great benefit for industry and trade

Revolution in Earth Science

Most valuable space technology

Main segments: GNSS

Space segments : GNSS satellites

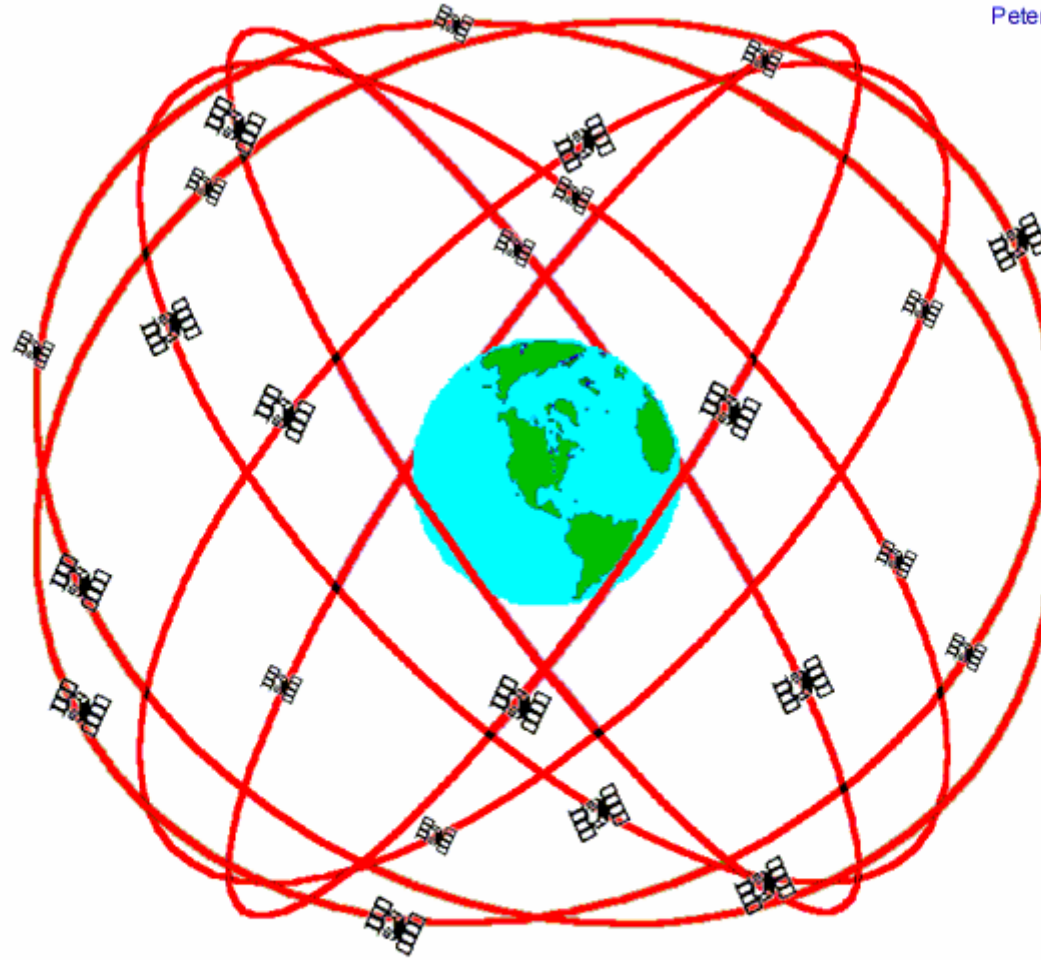
Ground segments : control stations

User segments : GNSS receivers

GNSS satellites

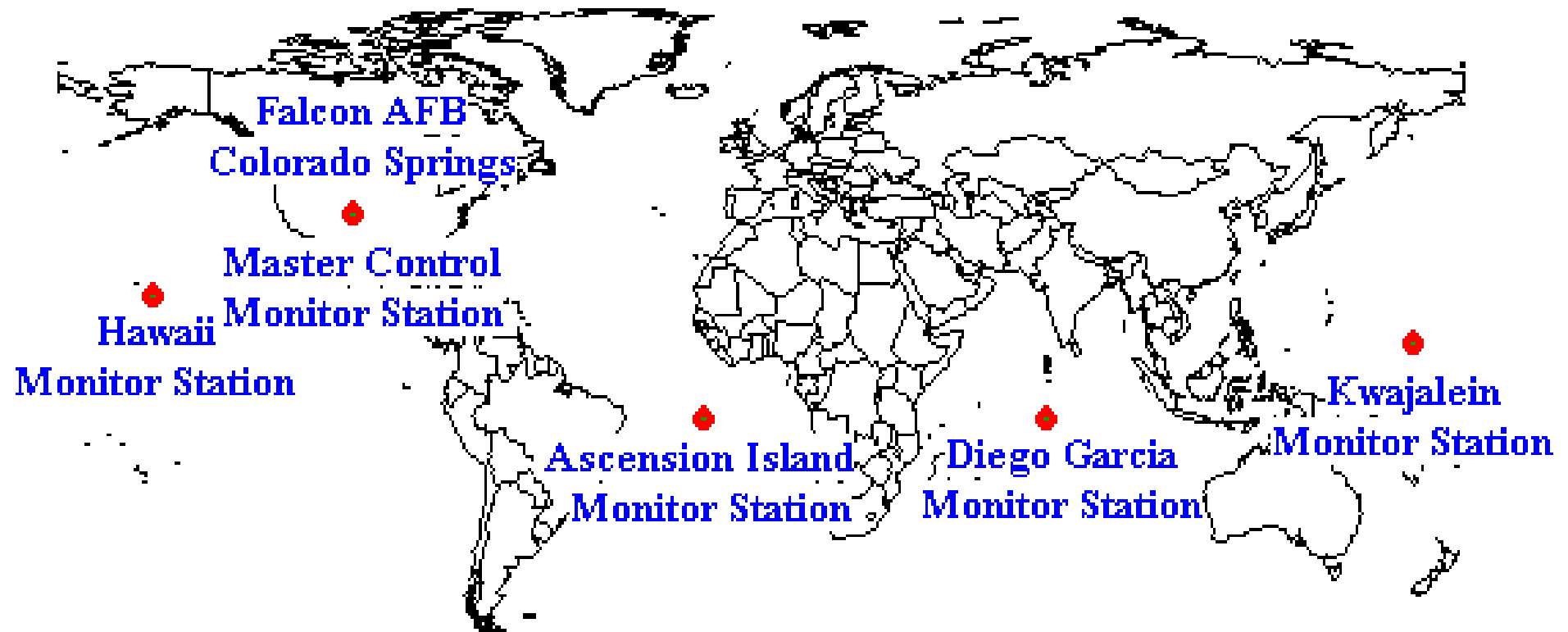
GPS constellation

Peter H. Dana 9/22/98



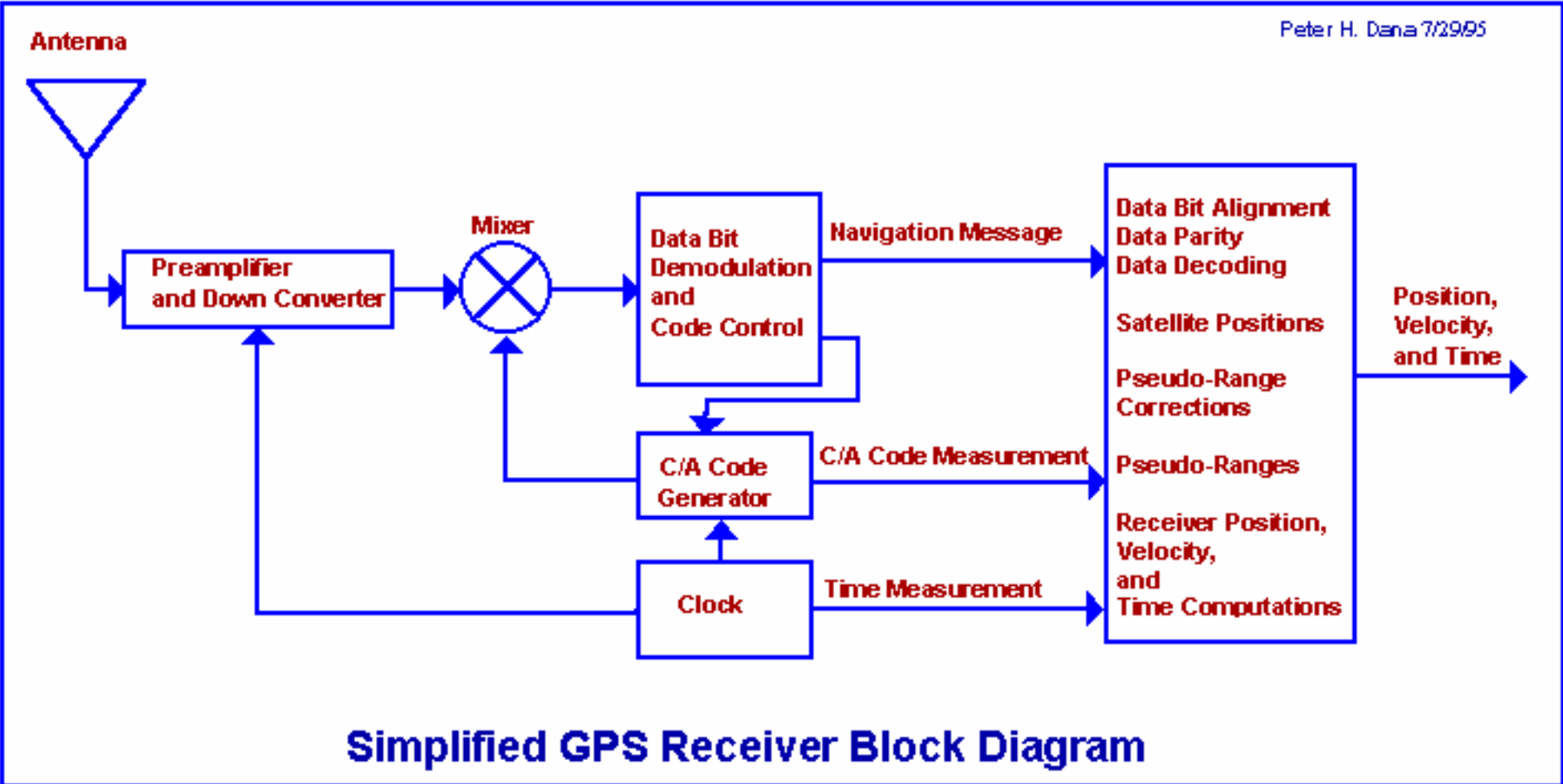
GPS Nominal Constellation
24 Satellites in 6 Orbital Planes
4 Satellites in each Plane
20,200 km Altitudes, 55 Degree Inclination

Ground control and monitor stations

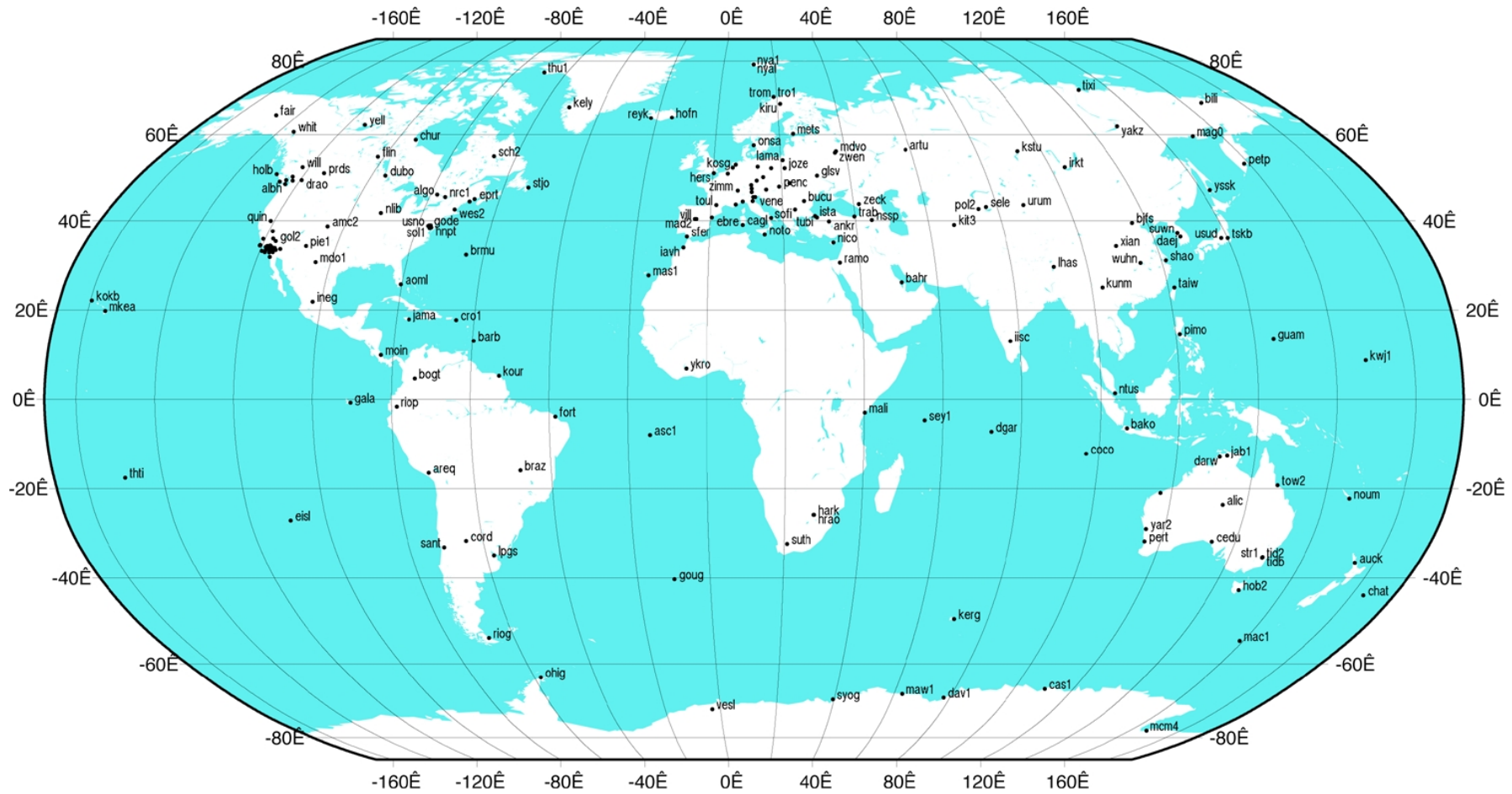


Global Positioning System (GPS) Master Control and Monitor Station Network

GNSS receivers

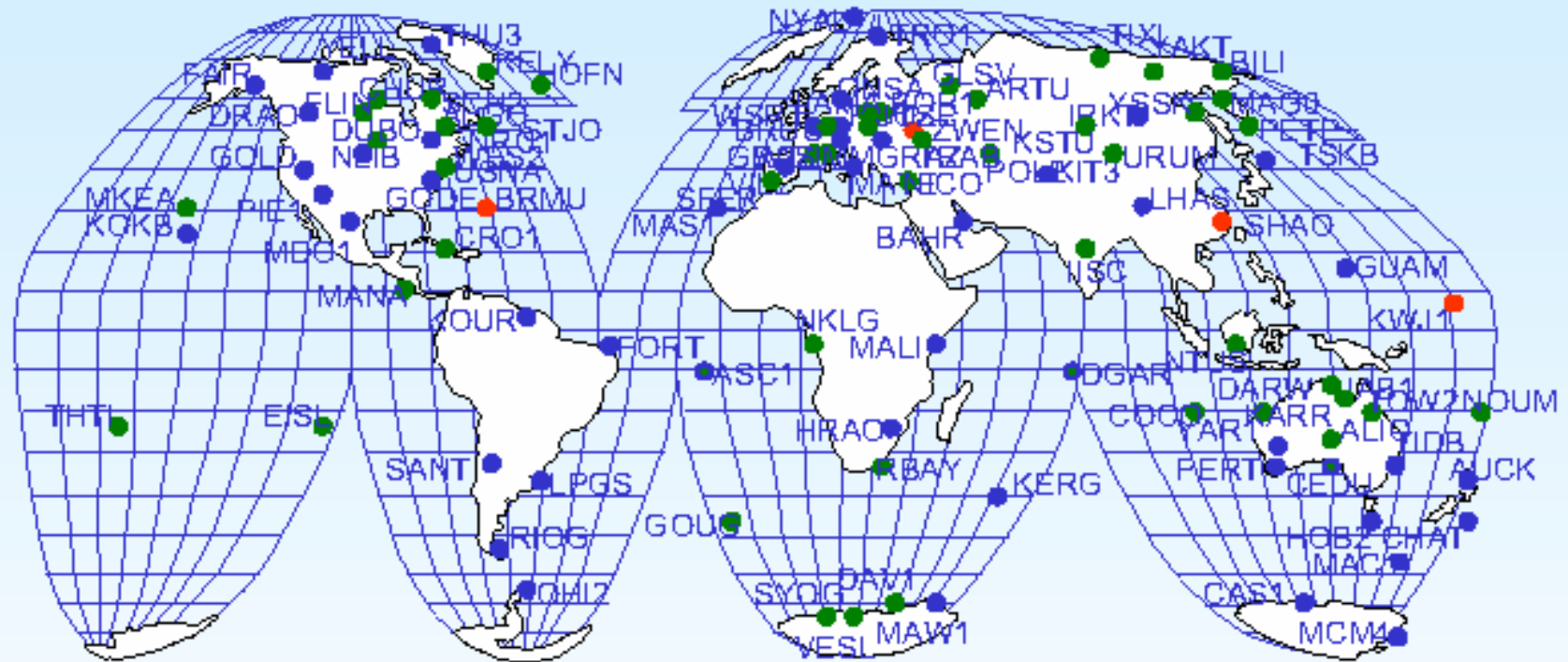


Simplified GPS Receiver Block Diagram



Global GNSS network

IGb00 Realization of ITRS



- Tracking Sites used for IGS00 but Removed for IGb00 (4) OHIG → OH12
THUI → THU3
TROM → TRO1
- Tracking Sites Added to IGS00 (49)
- Tracking Sites used for IGS00 and IGb00 (47)

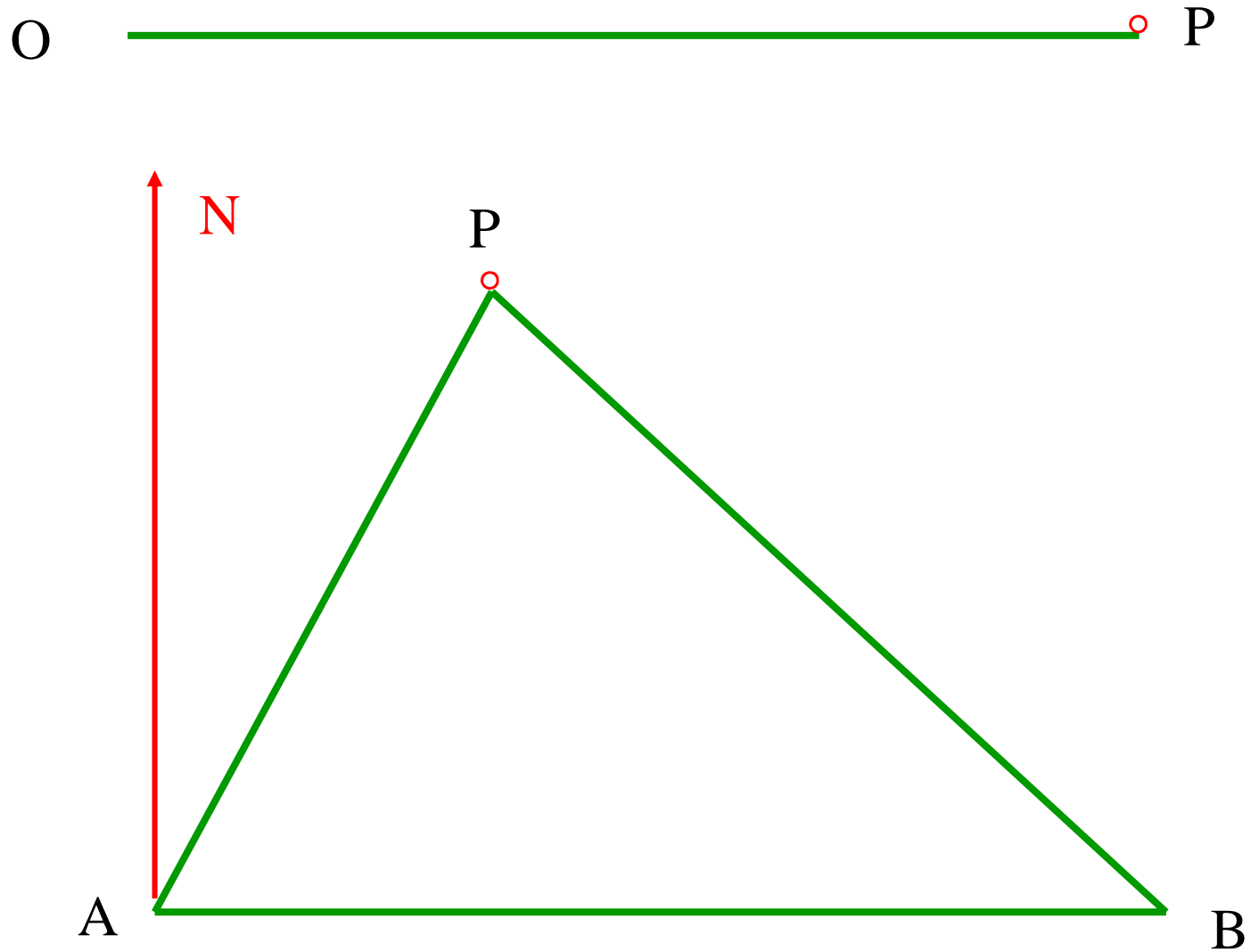
2Principle of positioning and data processing

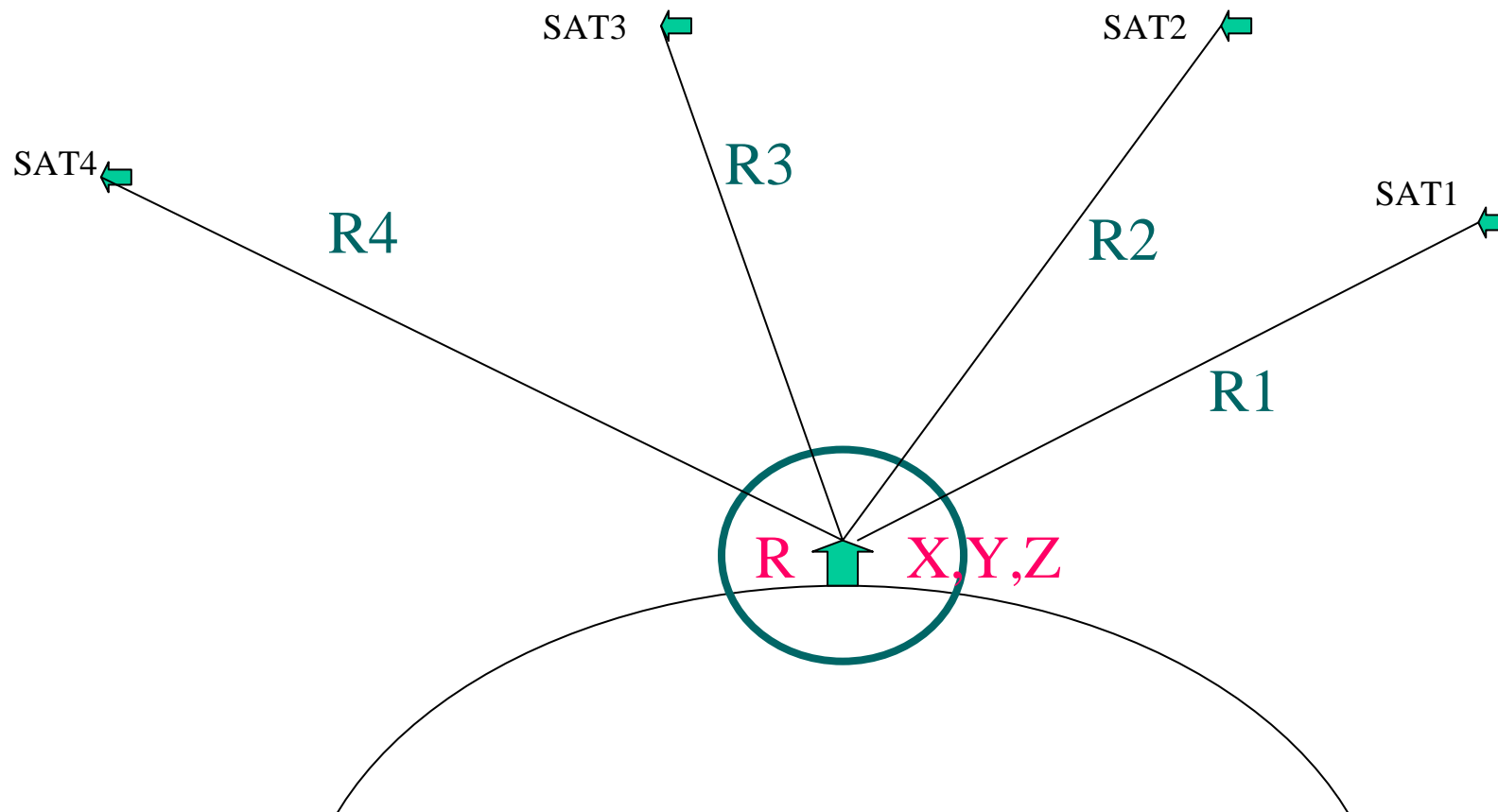
Principle of positioning

Kinematic and static positioning

2 Principle of positioning

Principle of positioning : positioning in one dimensional space and two dimensional space





$$R = ((x_r - x_s)^2 + (y_r - y_s)^2 + (z_r - z_s)^2)^{1/2} + \Delta \tau$$

Principle of GNSS positioning

Coordinate Conversion

Geodetic Latitude, Longitude, and Height to ECEF, X, Y, Z

$$X = (N + h) \cos \phi \cos \lambda$$

$$Y = (N + h) \cos \phi \sin \lambda$$

$$Z = [N(1 - e^2) + h] \sin \phi$$

where:

ϕ, λ, h = geodetic latitude, longitude, and height above ellipsoid

X, Y, Z = Earth Centered Earth Fixed Cartesian Coordinates

and:

$N(\phi) = a / \sqrt{1 - e^2 \sin^2 \phi}$ = radius of curvature in prime vertical

a = semi-major earth axis (ellipsoid equatorial radius)

b = semi-minor earth axis (ellipsoid polar radius)

$$f = \frac{a - b}{a} = \text{flattening}$$

$$e^2 = 2f - f^2 = \text{eccentricity squared}$$

Coordinate Conversion: Cartesian (ECEF X, Y, Z) and Geodetic (Latitude, Longitude, and Height)

Direct Solution for Latitude, Longitude, and Height from X, Y, Z

This conversion is not exact and provides centimeter accuracy for heights < 1,000 km

(See Bowring, B. 1976. Transformation from spatial to geographical coordinates.

Survey Review, XXIII: pg. 323-327)

$$\phi = \text{atan}\left(\frac{Z + e'^2 b \sin^3 \theta}{p - e'^2 a \cos^3 \theta}\right)$$

$$\lambda = \text{atan2}(Y, X)$$

$$h = \frac{P}{\cos(\phi)} - N(\phi)$$

where:

ϕ, λ, h = geodetic latitude, longitude, and height above ellipsoid

X, Y, Z = Earth Centered Earth Fixed Cartesian coordinates

and:

$$p = \sqrt{X^2 + Y^2} \quad \theta = \text{atan}\left(\frac{Za}{pb}\right) \quad e'^2 = \frac{a^2 - b^2}{b^2}$$

$N(\phi) = a / \sqrt{1 - e^2 \sin^2 \phi}$ = radius of curvature in prime vertical

a = semi - major earth axis (ellipsoid equatorial radius)

b = semi - minor earth axis (ellipsoid polar radius)

$$f = \frac{a - b}{a} = \text{flattening}$$

$$e^2 = 2f - f^2 = \text{eccentricity squared}$$

3 Measurements and measurement equations

Ambiguity, cycle slip

4 Error source

Orbit

Ionosphere delay

Troposphere delay

Phase centers of satellite antenna and receiver antenna

Multipath

Clock error(Sat. and RCV)

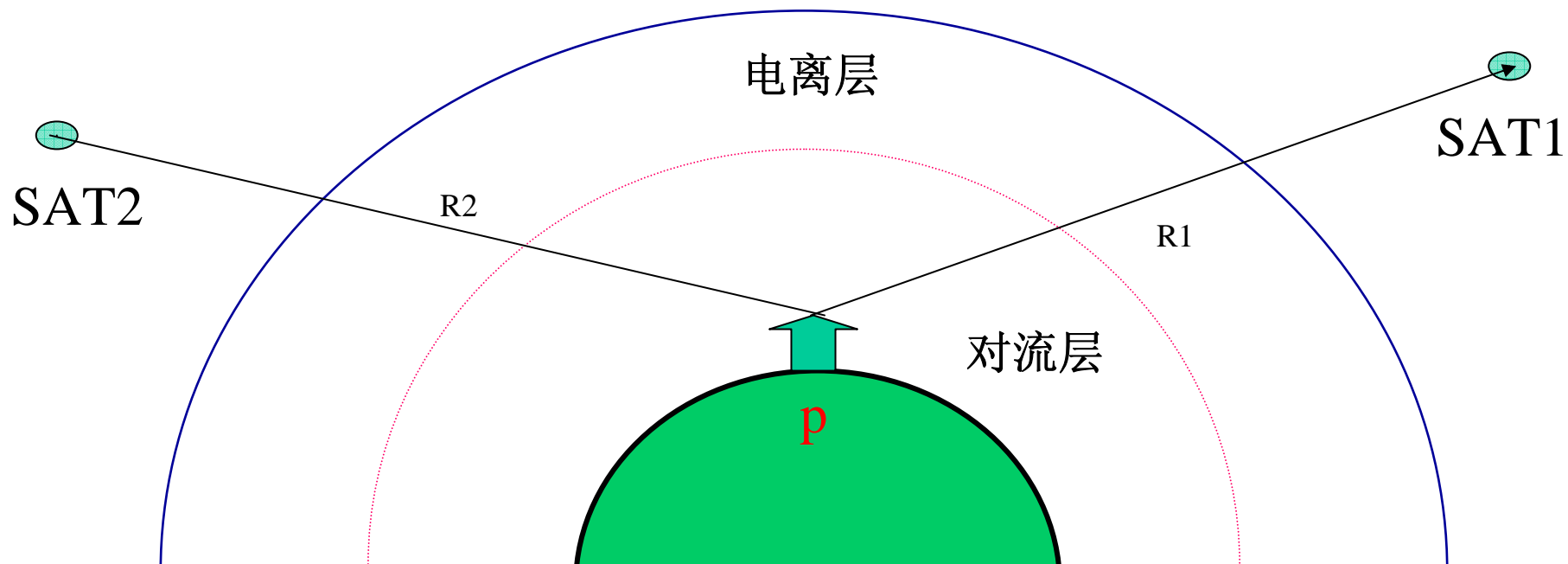
**Displacement tides (Earth tide, pole tide, ocean loading,
atmosphere loading**

Phase wind-up

Relativity effect

Known coordinates

Antenna centering



卫星轨道误差
 卫星钟差
 卫星天线相位中心偏差
 相对论效应

天线相对旋转
 相位增加效应

接收机钟差
 多路径效应
 接收机天线相位中心偏差
 固体潮
 极潮
 海水负荷
 对中误差 (对点误差)
 已知点点位误差

GPS相对定位误差源

GPS 卫星轨道

Precision in GPS results

Precision of GPS satellite orbits



5 Time and coordinate system

GPS time

UTC

GPS week

reference frame----foundation of geodetic results

WGS84

ITRF from ITRF89 to ITRF2005

IGS IGS05

6 Data processing and software

Differencing, linear combinations

Zero difference

Single difference

Double difference

Triple difference

Ionosphere-free observations

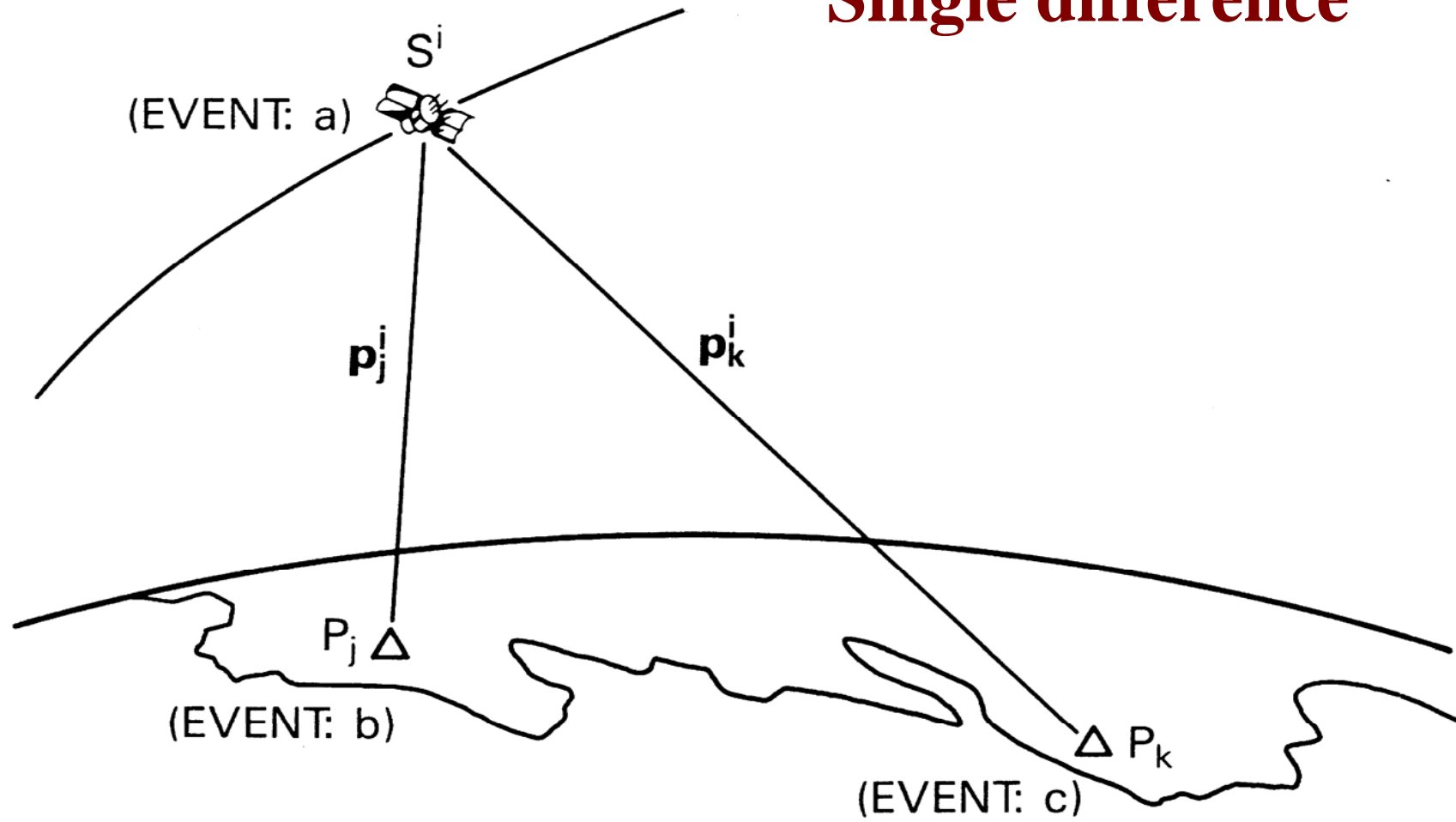
Geometry-free observations

GIPSY/OASIS

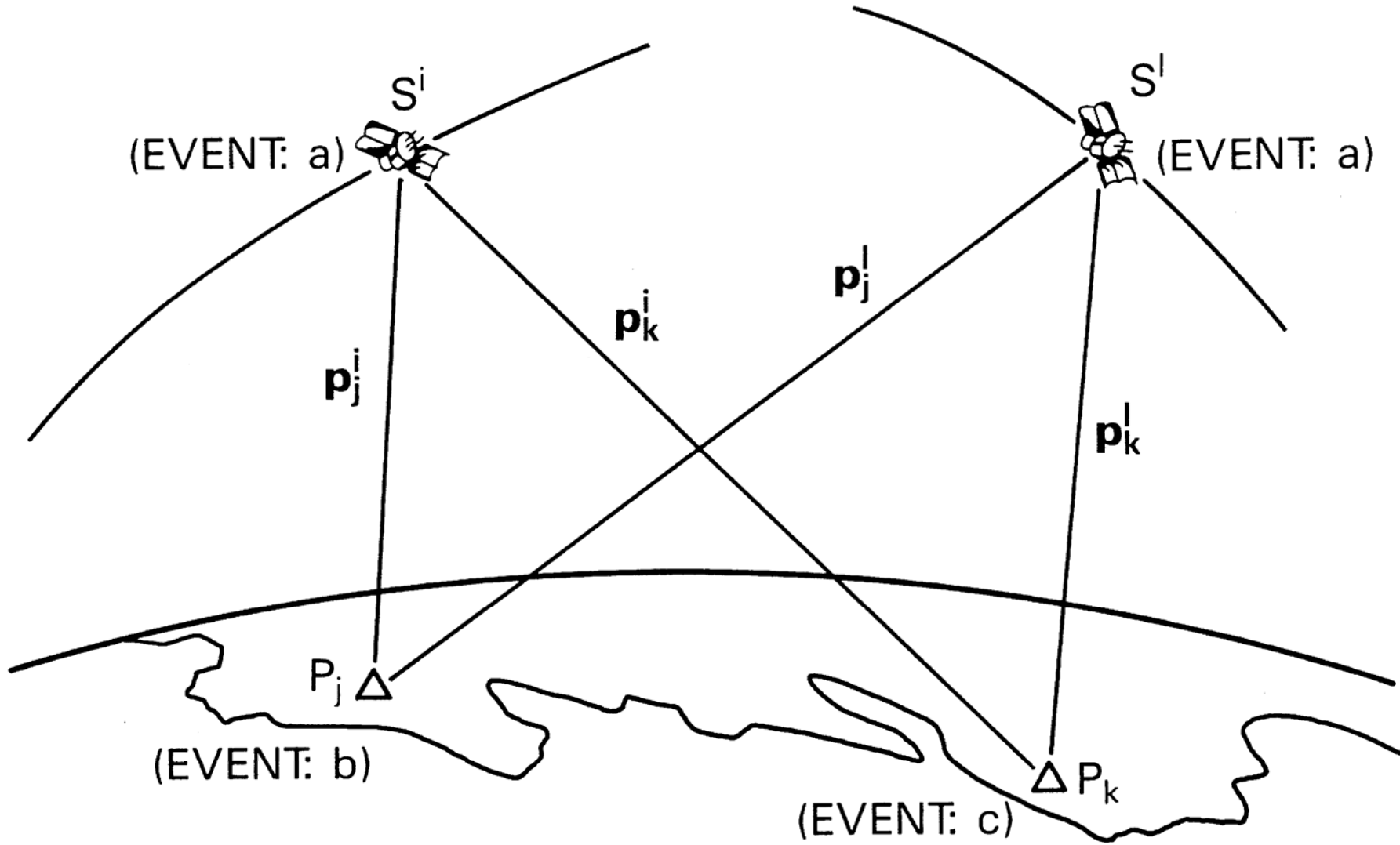
GAMIT/GLOBK

BERNESE

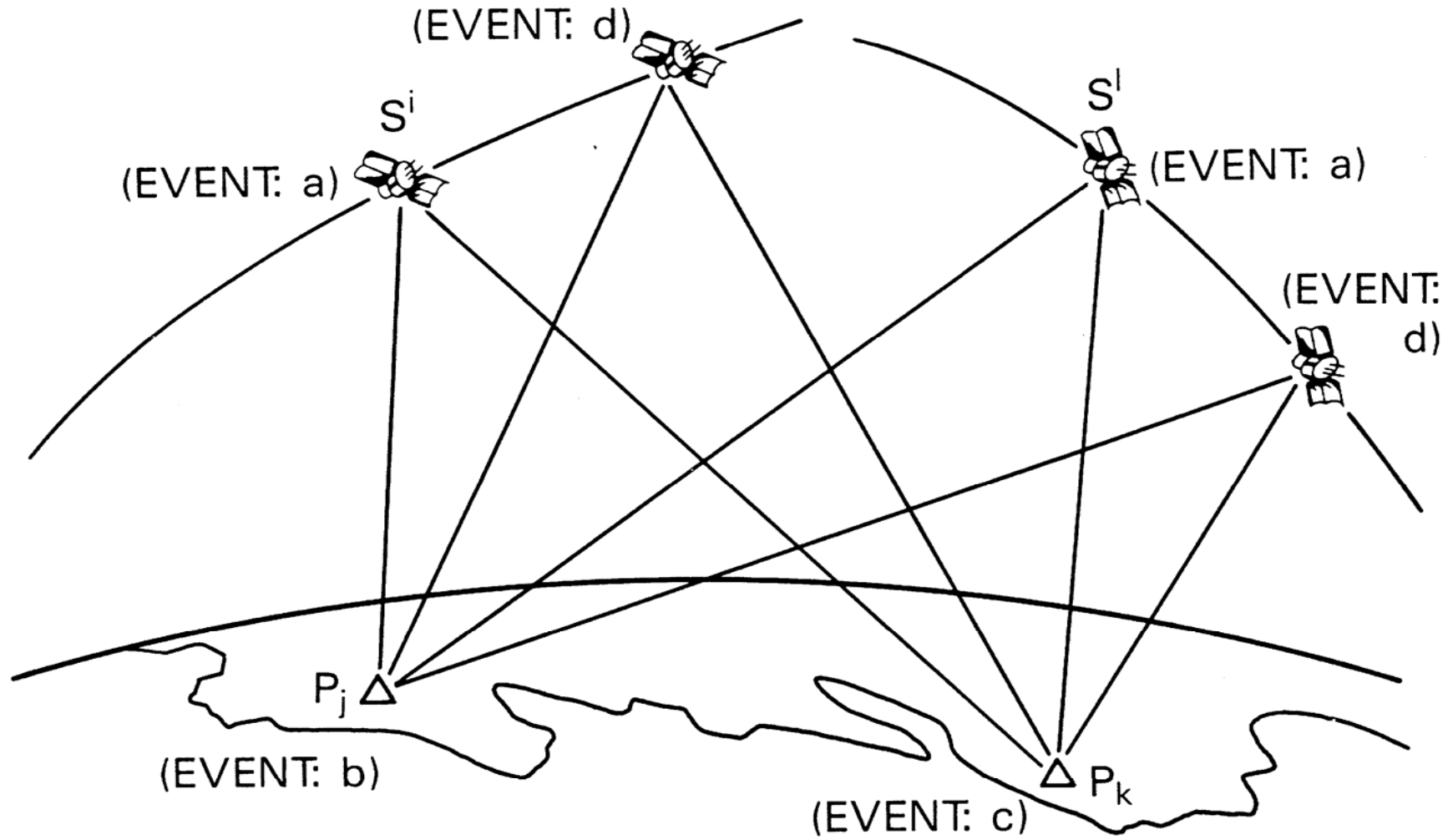
Single difference



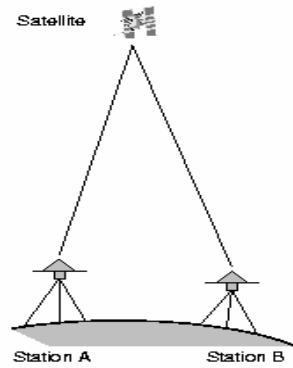
Double difference



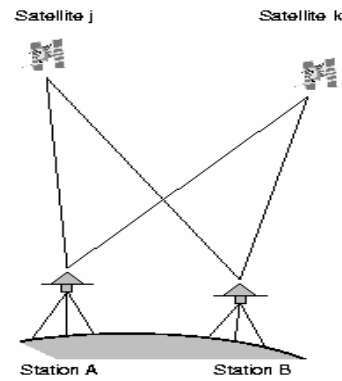
Triple difference



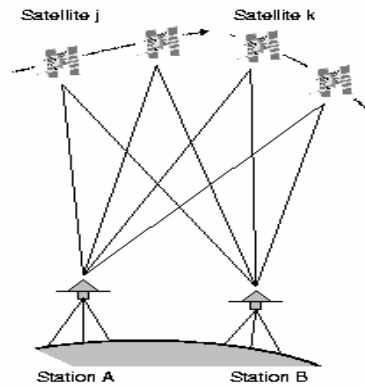
DIFFERENCING: ILLUSTRATIONS



Single Differences



Double Differences



Triple Differences

7 Application of GNSS (GPS) in Earth Science

Geodesy

Geodynamics----plate motion

Space physics----ionosphere monitoring

Meteorology----water vapor monitoring

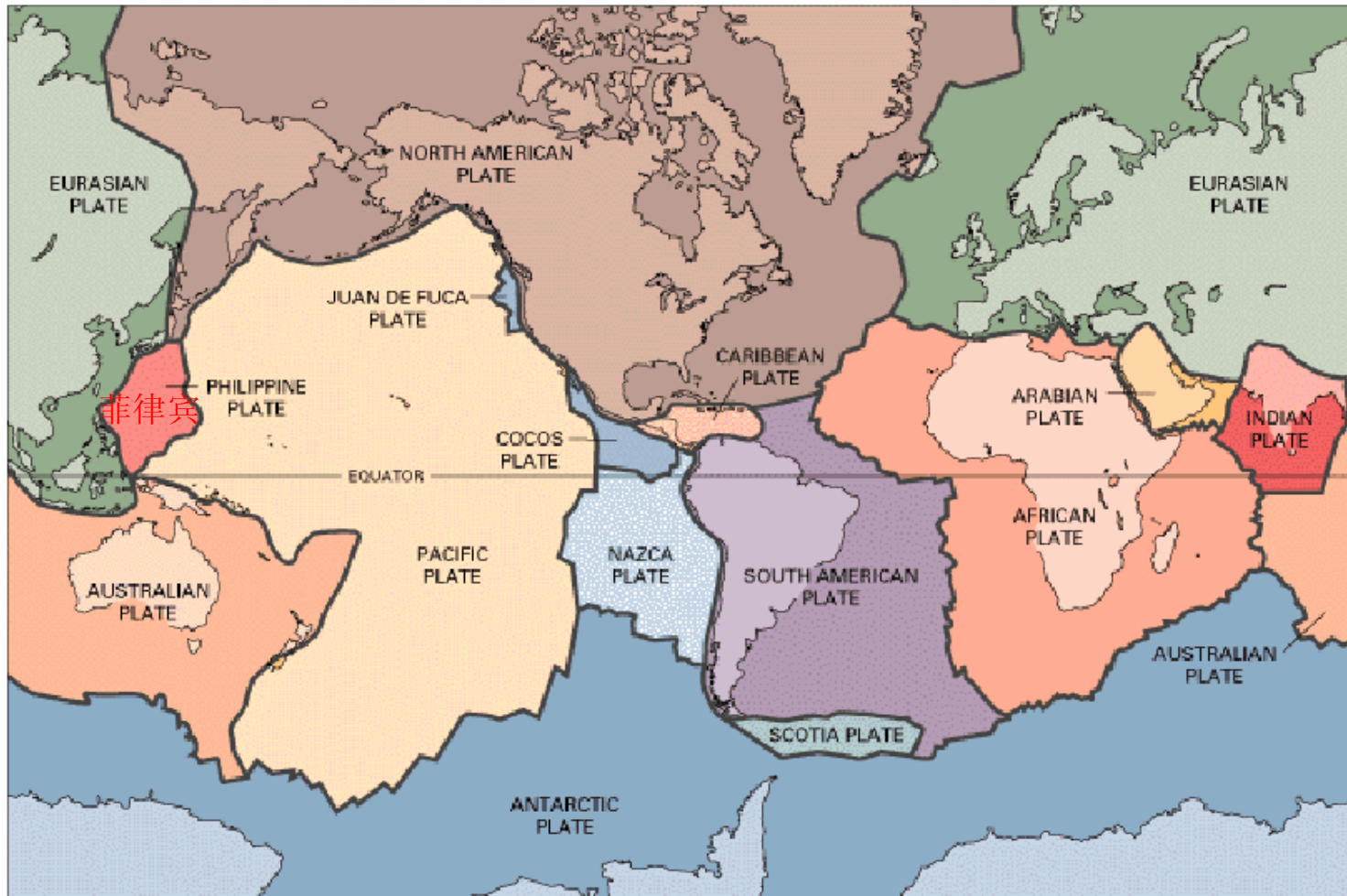
**Crustal movement----earthquake prediction,
volcanic activity, land subsidence, land slides**

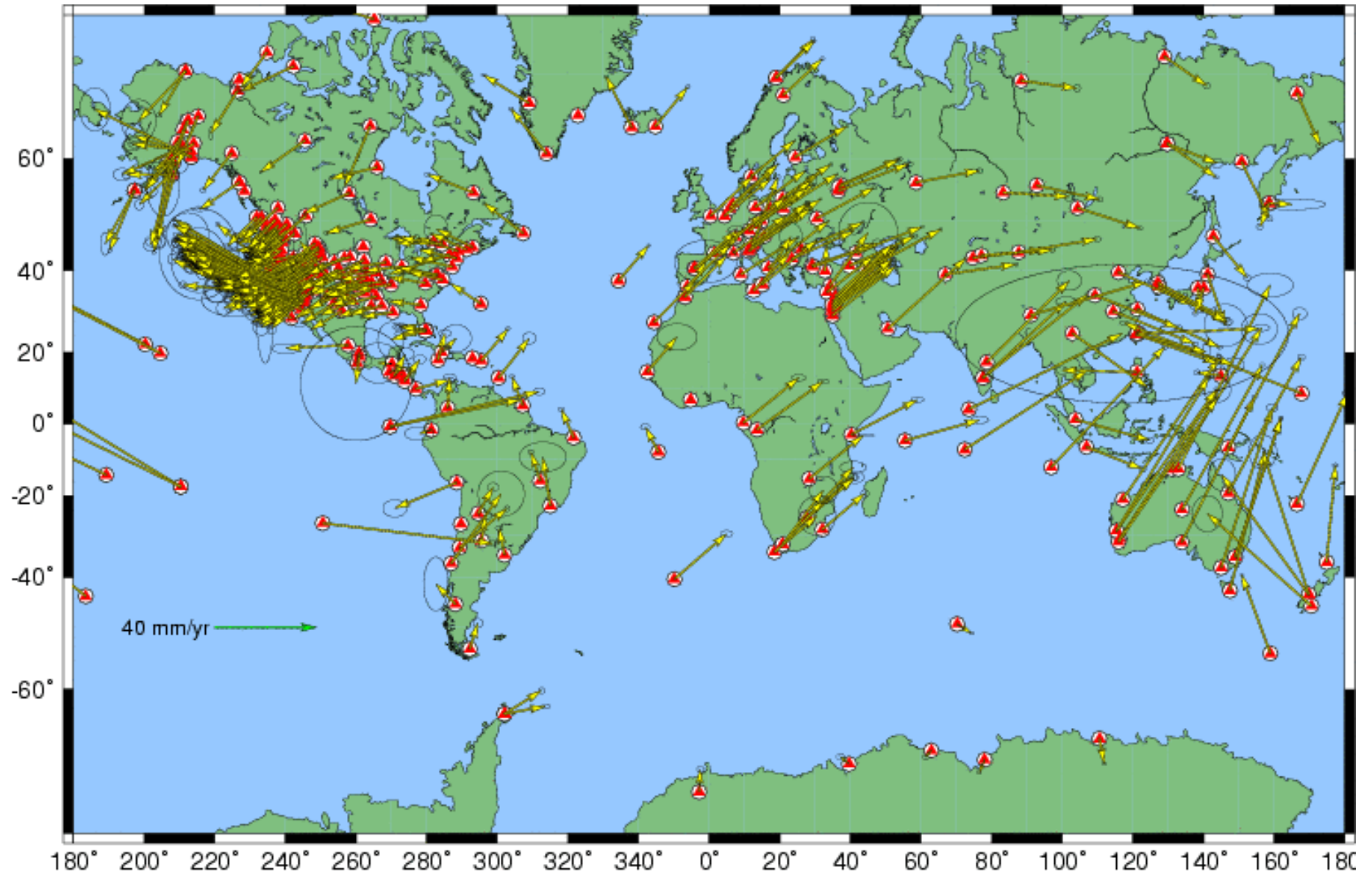
Sea level change

**Satellite orbit determination for deferent
missions for earth science**

Seismicity、 plates and plate motion

Tectonic Plates





GMT 2004 May 8 23:39:21 AREA: GLOBAL OVERVIEW

FRAME: ITRF2000

ERRORS: 95% CONFIDENCE ELLIPSES

NOISE MODEL: WHITE + FLICKER

2004,5,9 SIO

Plate motion

Horizontal Displacement on Chinese Mainland

Crustal movement

8 Conclusion

Thank you !