



Intermediate reference frame for Uzbekistan topographic maps

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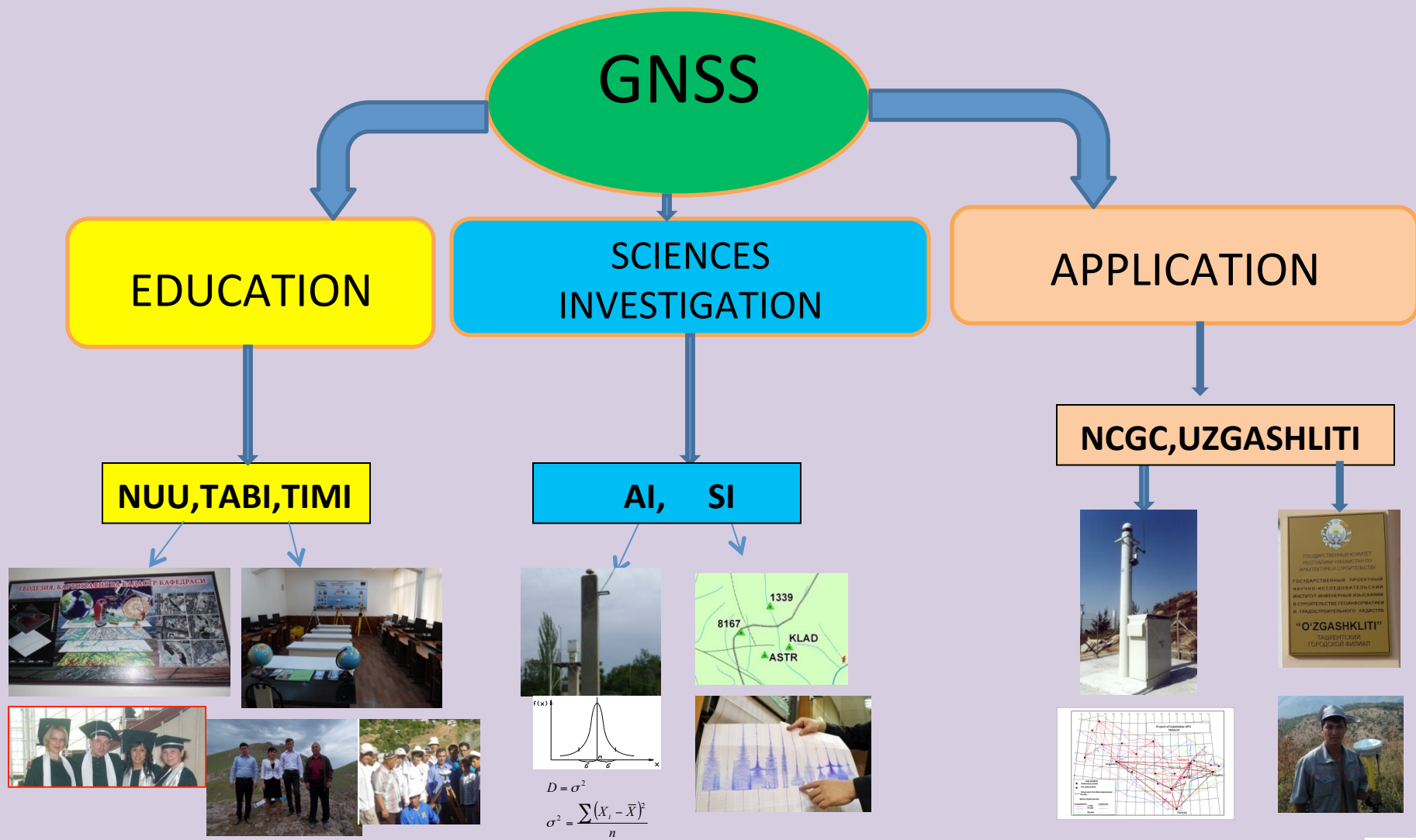




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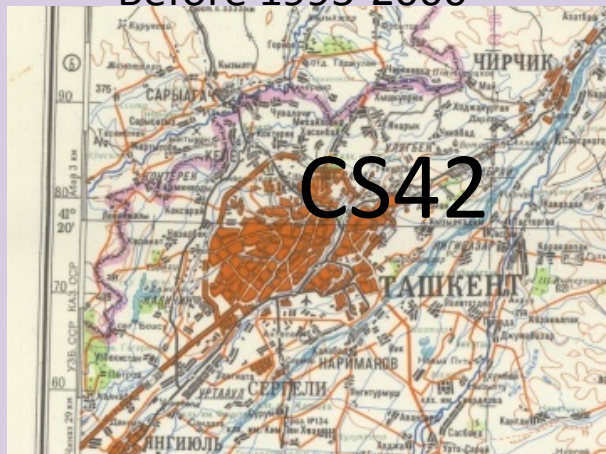




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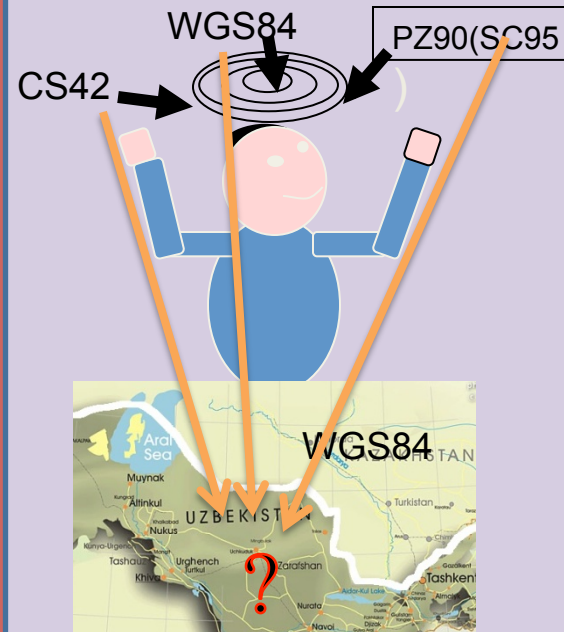
Before 1995-2000



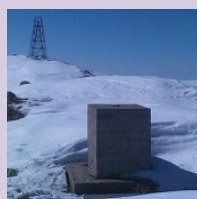
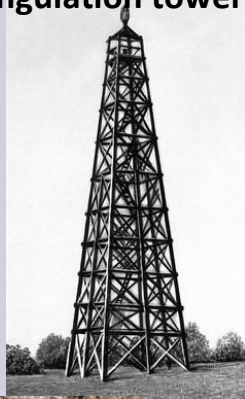
Now



In the future



Triangulation tower



BENCH MARK

United Nations/Russian Federation Workshop on the Applications of Global Navigation Satellite Systems, Krasnoyarsk, 18-22.05.2015





Tashkent coordinate system

Central Asian triangulation measurement were produced in Tashkent coordinate system (1875). This works are based on the Bessel –ellipsoid (1841), $a=6\,377\,397\text{m.}$, $\alpha=1/299.14$

The were measurement and calculated the longitude for 900 points ($\text{rms}=\pm 0^{\text{s}}.25$).



Gedeonov D.D 1854-1908



In 1950 about 50% of the European triangulation networks and about 20% of other continents networks (also **Russia** and **Uzbekistan**) were based on the Bessel ellipsoid.

$\lambda=-4^{\text{h}}37^{\text{m}}10.80^{\text{s}}$ 1891
 $\varphi =41^{\circ}19'31''.48$ 1895-1896





COORDINATE SYSTEM CS-32

Origin: Sablino, Russia.1930.

Bessel reference ellipsoid

$$a=6377397.155m$$

$$b=6356078.963$$

$$f=1:298,3.$$

$$\Delta X=382m.$$

$$\Delta Y=151m.$$

$$\Delta Z=574m.$$

$$\Delta a=739.845$$

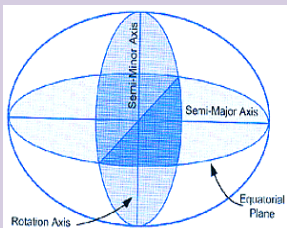
$$\Delta f= 0.10037483$$



Bessel F.V.
(1784-1846)



Pulkovo



COORDINATE SYSTEM CS-42

Origin: Bugry, Russia.1942.

Krasovsky reference ellipsoid

$$a=6378245m \quad b=6356863 \quad f=1/298.3$$

Resolution of the SU government, №760, 1946.04.07.

Astronomy- geodetic network (87 polygons) of 1 order

$$B_0 = \varphi_0 - \xi_0 = 59^{\circ} 46' 18''.71 - 0''.16 = 59^{\circ} 46' 18''.55$$

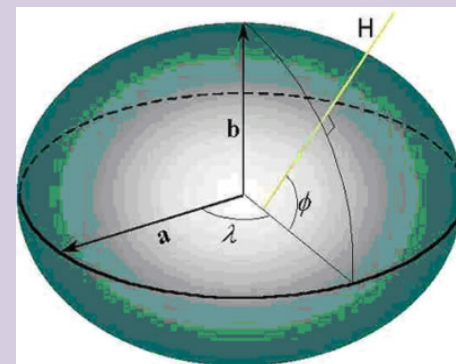
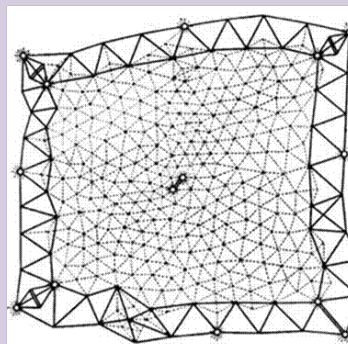
$$L_0 = \lambda_0 - \eta_0 \sec B_0 = 30^{\circ} 19' 38''.55 + 3''.54 = 30^{\circ} 19' 42''.09$$

$$A_0 = \alpha_0 - \eta_0 \operatorname{tg} B_0 = 121^{\circ} 40' 36''.13 + 2''.66 = 121^{\circ} 40' 38''.79 \text{ (Bugry)}$$

$$\xi_{0=} = -dB_0 = 0,16'', \quad \eta_0 \sec B = -dL_{0=} = -3,54'', \quad \eta_0 = 1,78''.$$



Krasovsky
1878-1948



Triangulation line 1ord



Triangulation line 2ord



Base-line

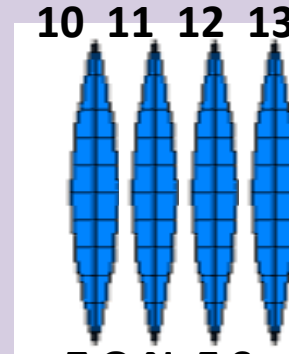
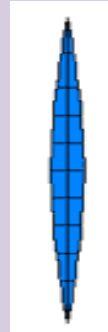
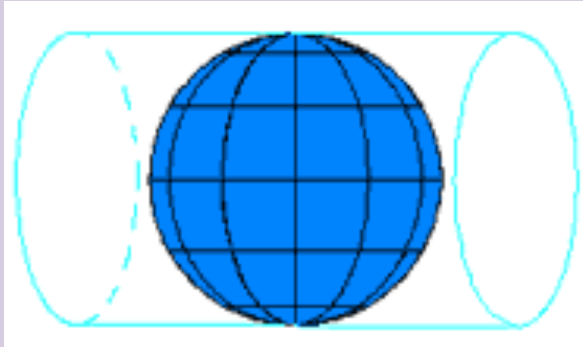


Astronomical points





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THE GAUSS-KRÜGER PROJECTION



**ZONES
UZBEKISTAN**



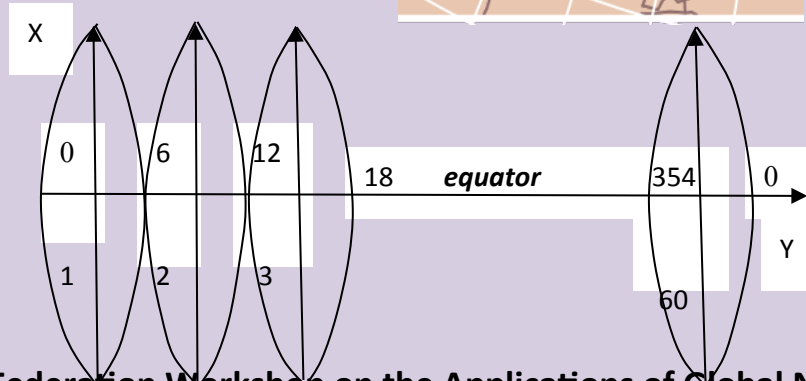
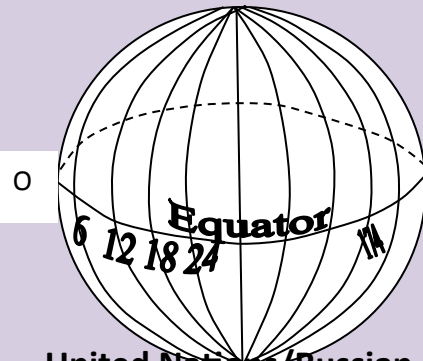
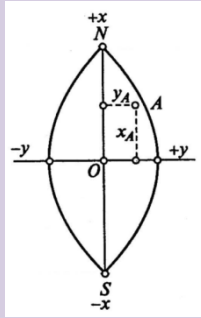
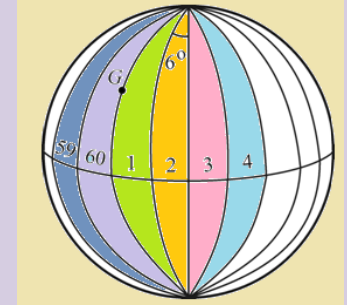
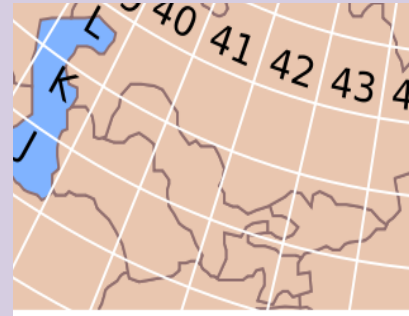
J. Krüger
1853-1923

Gauss K F
(1777 – 1855)

$$x = S + \frac{l^2}{2} r \sin B + \frac{l^4}{24} r \cos^2 B \sin B (5 - t^2 + 9\eta^2 + 4\eta^4);$$

$$y = lr + \frac{l^3}{6} r \cos^2 B (1 - t^2 + \eta^2) + \frac{l^5}{120} r \cos^4 B (5 - 18t^2 + t^4 - 14\eta^2 - 58\eta^2 t^2);$$

$$m = n = 1 + 0,000152l^2 \cos^2 B; \quad p = m^2; \quad w = 0; \quad t = \operatorname{tg} B; \quad \eta^2 = e'^2 \cos^2 B,$$



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SK42(Pulkovo)



SK42, WGS84

$$B_0 = \varphi_0 - \xi_0$$

$$L_0 = \lambda_0 - \eta_0 \sec B_0$$

$$A_0 = \alpha_0 - \eta_0 \operatorname{tg} B_0$$

$$y_{\text{wgs84}} - y_{\text{sk42}} = 64\text{m.}, L_{\text{wgs84}} - L_{\text{sk42}} = 2.90 \text{ arcsec}$$

$$x_{\text{wgs84}} - x_{\text{sk42}} = 9\text{m.}, B_{\text{wgs84}} - B_{\text{sk42}} = 0.23 \text{ arcsec}$$

$$h_{\text{wgs84}} - h_{\text{sk42}} = 109\text{m}$$

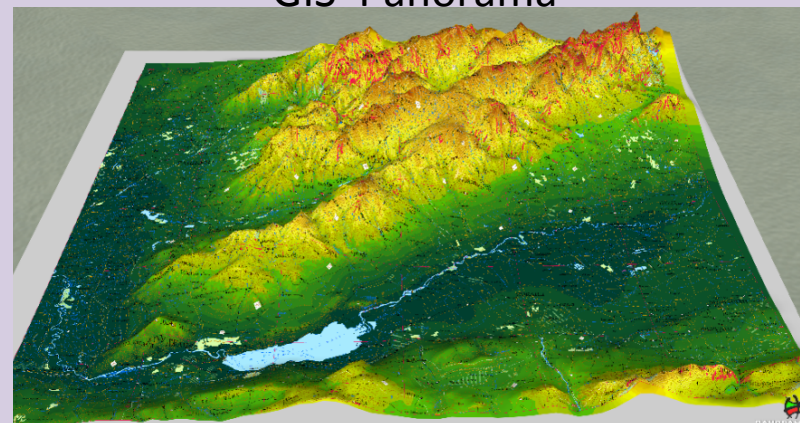
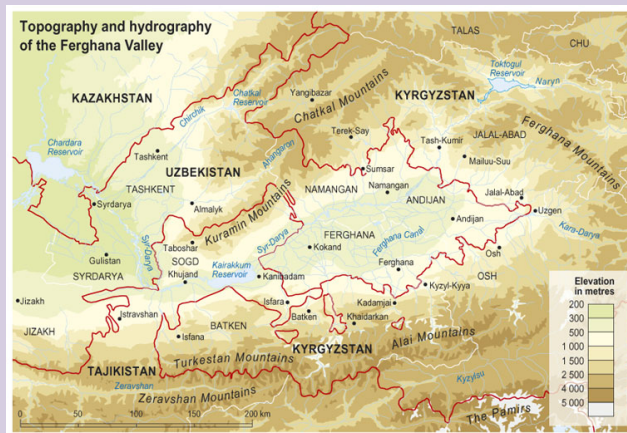
Scale	$\Delta X_{\text{wgs84-sk42}}$	$\Delta Y_{\text{wgs84-sk42}}$
1:100 000	0.09mm	0.64mm
1:50 000	0.18mm	1.28mm
1:25 000	0.30mm	2.56mm
1:10 000	0.9mm	6.40mm
1:5 000	1.8mm	12.8mm





The first geoid

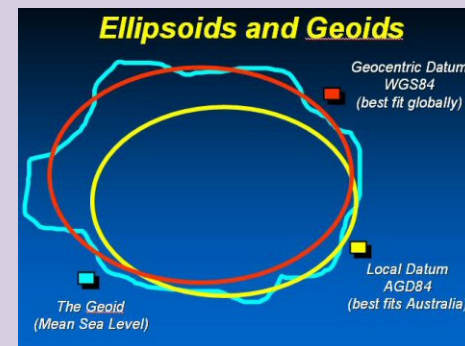
GIS Panorama



Ferghana valley

Prof. Pomeranzev
1847-1921

The geoid of Ferghana valley (1897).
 $B-\phi=12.73''$, $L-\lambda=16.31''$, $Rms=\pm 0.30''$
33 points.

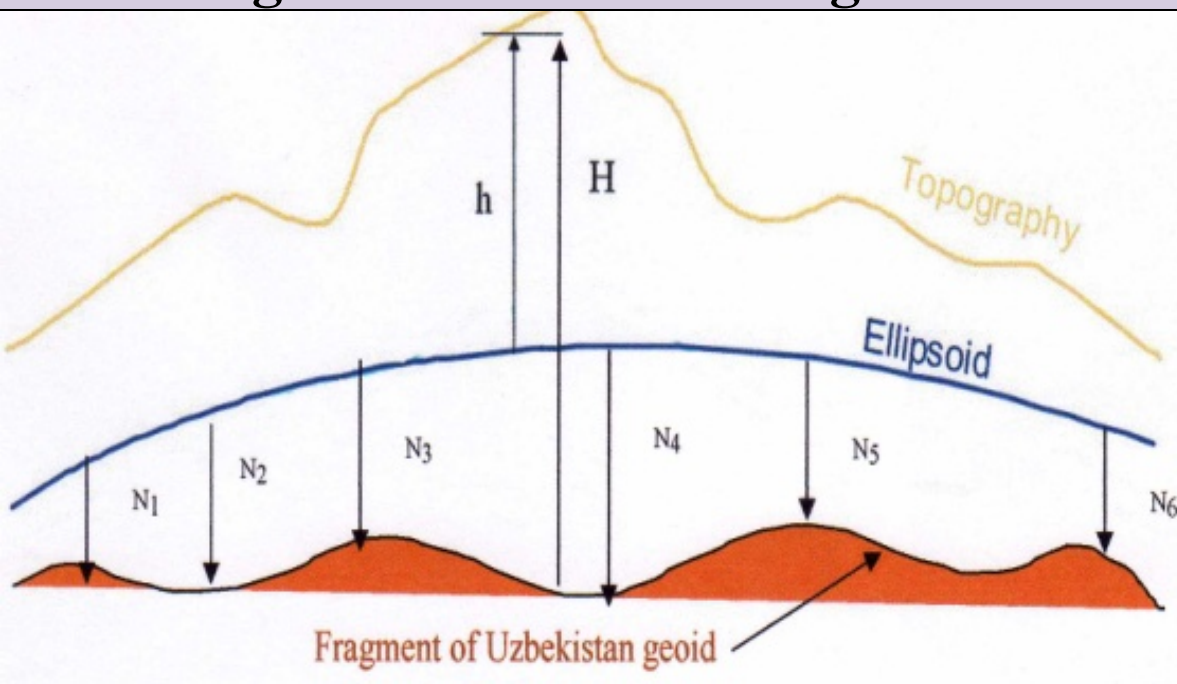


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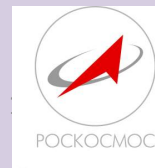
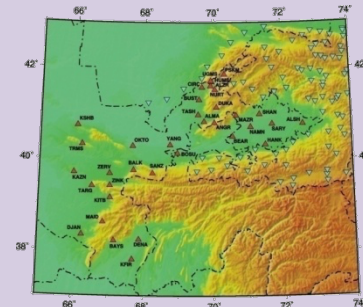
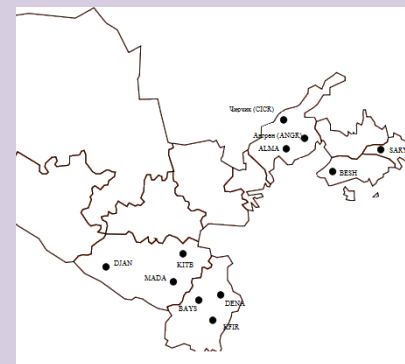
Fragment of Uzbekistan geoid

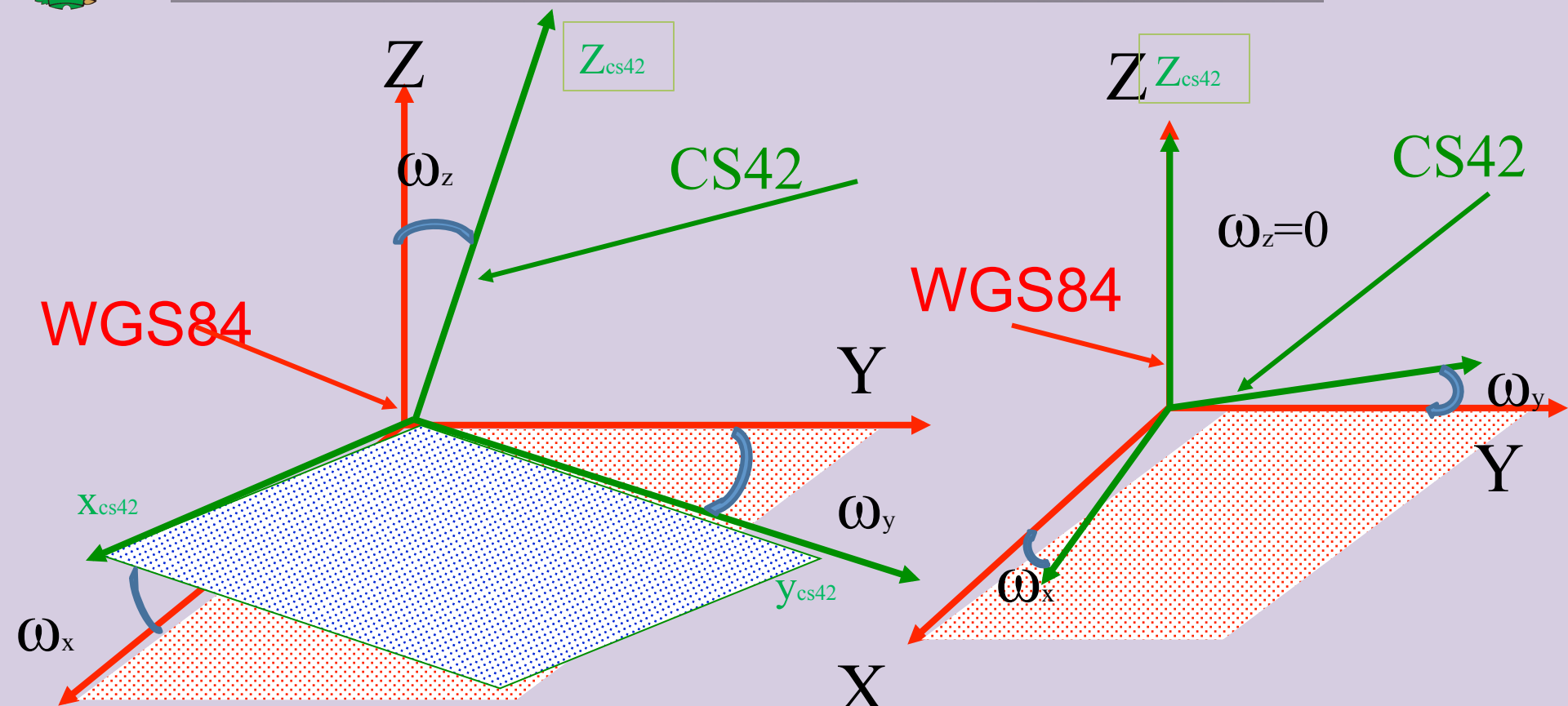


$$N = \frac{GM}{\rho\gamma_0} \left[1 + \sum_{n=2}^{\infty} \sum_{m=0}^n \left(\frac{a}{\rho} \right)^n P_{nm}(\sin \varphi_e) \times (C_{nm} \cos m \lambda_e + S_{nm} \sin m \lambda_e) \right]$$

CATS network (Uzbekistan)(1992-1996)

No _{CT}	N _z M
1	-37.73
2	-36.71
3	-40.14
4	-41.37
6	-36.96
9	-41.60
10	-42.90
16	-50.97
40	-35.64
54	-40.41
55	-42.86
56	-46.79
58	-37.90
60	-43.85
61	-43.16





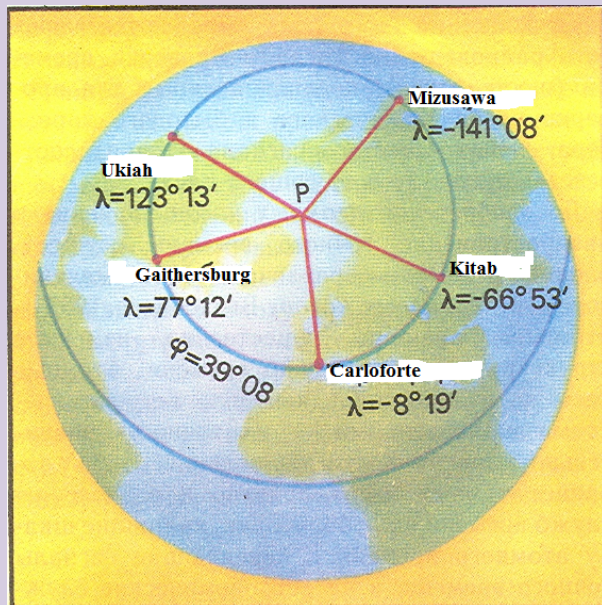
$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{SK-42} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{WGS-84} + \begin{bmatrix} T_X \\ T_Y \\ T_Z \end{bmatrix} + \begin{bmatrix} m & \omega_Z & -\omega_Y \\ -\omega_Z & m & \omega_X \\ \omega_Y & -\omega_X & m \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{WGS-84}$$

DATUM	ΔX	ΔY	ΔZ	Method	Comments
CS42-WGS84	+28	-130	-95	Molodensky	NIMA
CS42-WGS84	+25	-141	-80	Helmert	GOST(RU)
CS42-WGS84	+22	-123	-83	Molodensky	Bazlov(RU)
CS42-WGS84	+23	-125	-87	Molodensky	Fazilova(UZ)

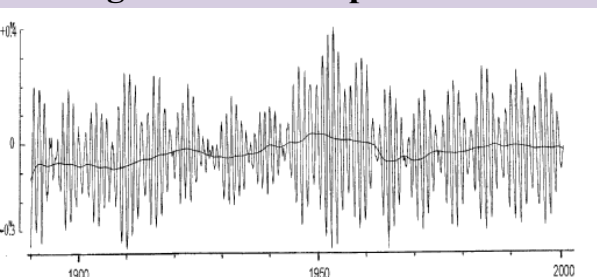




International Latitude station (1899)

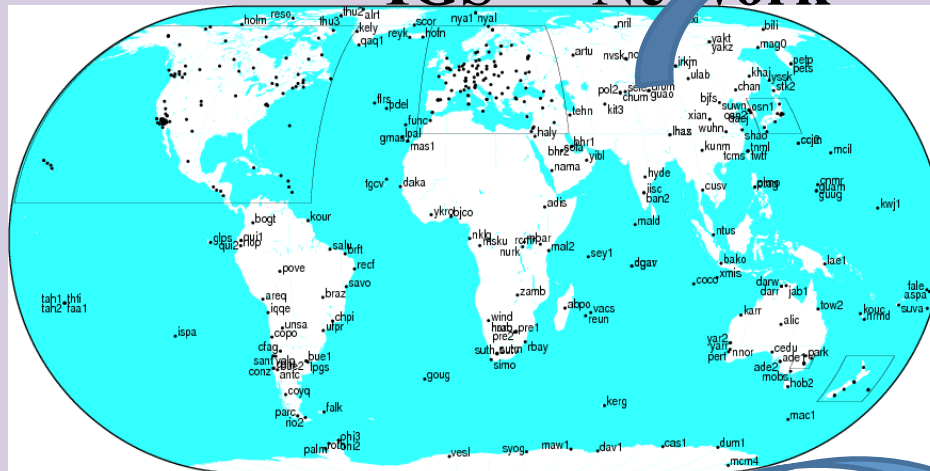


Change of the north pole coordinate



$$\begin{aligned} \varphi^* - \varphi &= x \cos \lambda - y \sin \lambda; \\ \lambda^* - \lambda &= (x \sin \lambda - y \cos \lambda) \operatorname{tg} \varphi; \\ \eta^* - \eta &= (\lambda^* - \lambda) \cos B; \\ A^* - A &= (x \sin \lambda - y \cos \lambda) \cos \varphi. \end{aligned}$$

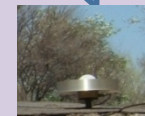
IGS Network



DORIS NETWORK



Kit3



Kitab, Uzbekistan

CHAMP



Tashkent



Kitab

MAID



Maidanpak





Transformation of coordinate system

$$\begin{aligned} x &= (N+H) \cos B \cos L \\ y &= (N+H) \cos B \sin L \\ z &= (N(1-e^2)+H) \sin B \end{aligned}$$

B, L, H, WGS84

X, Y, Z (WGS84)

X, Y, Z (CS42)

B, L, H, CS-42

x, y (CS42)
G-K projection

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{84} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{42} + \begin{bmatrix} T_X \\ T_Y \\ T_Z \end{bmatrix} + \begin{bmatrix} \mu & \omega_Z & -\omega_Y \\ -\omega_Z & \mu & \omega_X \\ \omega_Y & -\omega_X & \mu \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{42}$$

$$L = \arctg \frac{Y}{X} \quad B^{(i)} = \arctan \frac{Z + N^{(i-1)} e^2 \sin B^{(i-1)}}{r_p}$$

$$H = \sqrt{X^2 + Y^2} \times \sec B - N$$

$$\begin{aligned} x &= S + \frac{l^2}{2} r \sin B + \frac{l^4}{24} r \cos^2 B \sin B (5 - t^2 + 9\eta^2 + 4\eta^4); \\ y &= lr + \frac{l^3}{6} r \cos^2 B (1 - t^2 + \eta^2) + \frac{l^5}{120} r \cos^4 B (5 - 18t^2 + t^4 - 14\eta^2 - 58\eta^2 t^2); \\ m &= n = 1 + 0,000152l^2 \cos^2 B; \quad p = m^2; \quad w = 0; \quad t = tgB; \quad \eta^2 = e'^2 \cos^2 B, \end{aligned}$$

$$\begin{aligned} y_{wgs84} &= y_{sk42} + \Delta y \\ x_{wgs84} &= x_{sk42} + \Delta x \end{aligned}$$

Intermediate
G-K projection





REFERENCE FRAME

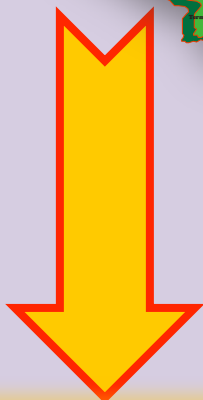
NATIONAL



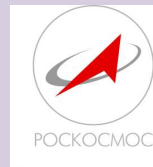
LOCAL(1+2 regions)

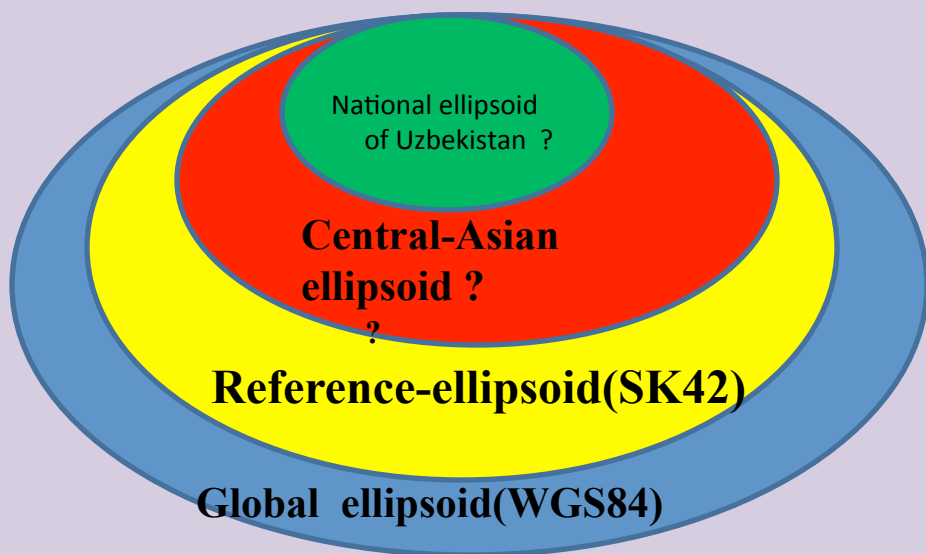
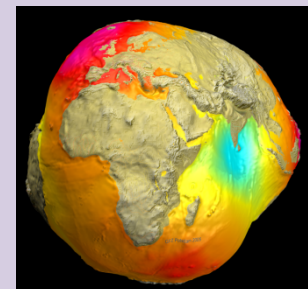
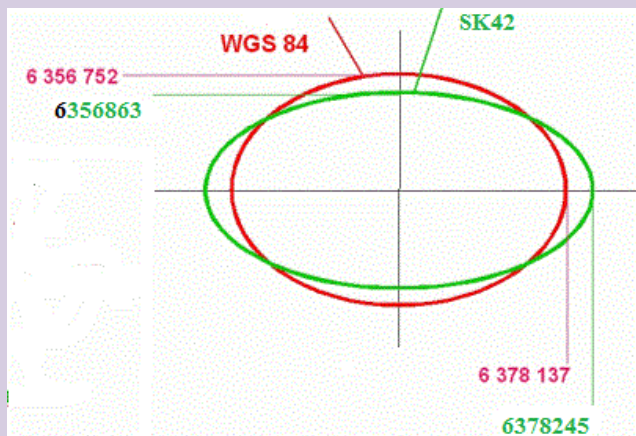


region



UZBEKISTAN







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