The NeQuick Ionospheric Electron Density Model and Space Weather

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• The NeQuick 2 (Nava et al., 2008) is an ionospheric electron density model developed at the T/ICT4D Laboratory of The Abdus Salam International Centre for Theoretical Physics (ICTP), Trieste, Italy, in collaboration with the Institute for Geophysics, Astrophysics and Meteorology (IGAM) of the University of Graz, Austria.

• It is a quick-run empirical model particularly designed for trans-ionospheric propagation applications, conceived to reproduce the median behavior of the ionosphere.

• [http://t-ict4d.ictp.it/nequick2](http://t-ict4d.ictp.it/nequick2)
NeQuick

- The model profile formulation includes 6 semi-Epstein layers with modeled thickness parameters and is based on anchor points defined by foE, foF1, foF2 and M(3000)F2 values.

- These values can be modeled (e.g. ITU-R coefficients for foF2, M(3000)F2) or experimentally derived.

- NeQuick inputs are: position, time and solar flux; the output is the electron concentration at the given location and time.

\[
N(h; h_{\text{max}}, N_{\text{max}}, B) = \frac{4N_{\text{max}}}{(1 + \exp\left(\frac{h - h_{\text{max}}}{B}\right))^2} \exp\left(\frac{h - h_{\text{max}}}{B}\right)
\]
NeQuick

- NeQuick package includes routines to evaluate the electron density along any “ground-to-satellite” ray-path and the corresponding Total Electron Content (TEC) by numerical integration.
Empirical models like NeQuick have been conceived to reproduce the median behavior ("climate") of the ionosphere.

For research purposes and practical applications, it is necessary to estimate the 3-D electron density of the ionosphere for current conditions ("weather").

Considering the increasing availability of experimental data even in real time, several assimilation schemes have been developed. They are of different complexity and rely on different kinds of data.

In the case of NeQuick, (multiple) effective parameters have been utilised to adapt the model to GNSS-derived TEC data (and ionosonde measured peak parameters values). In the following, specific examples will be outlined.
vTEC data ingestion

grid points:
lat.=-90°, 90° step 2.5°
lon.=-180°, 180° step 5°
Reconstructed foF2 map

grid points:
lat. = -90°, 90° step 2.5°
lon. = -180°, 180° step 5°
NeQuick2: validation results (example: HSA)

foF2 error statistics (Apr 2000)

Nava et al. (2011)
sTEC data ingestion; error statistics (000405)

Nava et al., 2006

Reconstructed STEC

Reconstructed foF2
foF2 data ingestion; error statistics, Sep 2011

"Weather"

Reconstructed foF2

"Climate"

Data as in Elvidge et al. (2014)
vTEC ingestion; geomagnetically disturbed period

vTEC at abj station during 5 quietest days (top) and 5 disturbed days (bottom) in 2015. TEC-GPS: black line; TEC-NeQuick 2 driven by R12: dashed blue line; TEC-NeQuick 2 driven by Rz: dashed red line; TEC-NeQuick 2 driven by the effective f10.7 as inferred from ykro data: green line with star symbol.

Yao et al., 2018
vTEC ingestion; geomagnetically disturbed period

Distribution of the differences between modeled and experimental vertical TEC during geomagnetically disturbed days (left) and quiet days (right) in 2015 at abj station. NeQuick 2 is driven by the daily sunspot number Rz (top) and the effective solar flux Az1 as inferred from ykro data (bottom).

Yao et al., 2018
Nevertheless, the first attempt to describe the ionospheric weather has been performed by merging monthly average foF2 (M(3000) F2) global maps with single epoch foF2 (M(3000)F2) grid-point measurements (Leitinger et al., 2001). This allowed generating “worst case” ionospheric scenarios (including geomagnetically disturbed conditions) for assessment of the operational ionospheric algorithms of EGNOS.
The BLUE algorithm

To further improve the NeQuick performance in retrieving the 3D electron density of the Ionosphere, a minimum variance least-squares estimation has also been utilised to assimilate ground and space-based TEC data into the model, considered as a background.

Best Linear Unbiased Estimator (BLUE)*

$y$ vector of observations
$x_b$ background model state
$x_a$ analysis model state
$H$ observation operator
$R$ covariance matrix of observation errors
$B$ covariance matrix of background errors
$A$ covariance matrix of analysis errors

*http://www.ecmwf.int/newsevents/training/rcourse_notes/DATA_ASSIMILATION/ASSIM_CONCEPTS/Assim_concepts2.html#962570
The BLUE algorithm

The optimal least-square estimator (BLUE analysis) is defined by

\[ x_a = x_b + K (y - Hx_b) \]
\[ K = BH^T (HBH^T + R)^{-1} \]
\[ A = (I-KH)B \]

In our case:

\[ y = \text{GNSS sTEC} \]
\[ x_b = \text{NeQuick electron density} \]
\[ x_a = \text{retrieved electron density} \]
\[ H \rightarrow \text{“crossing lengths” in “voxels”} \]

Simple formulation for \( B \) has been adopted (\( R \) is diagonal)
GNSS TEC DA - Example 1

• For the assimilation
  • Calibrated ground-based GNSS-derived slant TEC data from about 150 receivers of the LISN network (C. Valladares), located in the South American region.

• The data correspond the period 11-13 March 2011
LISN: 3 days data (2011/03/11-12-13)

Equivalent vertical TEC (LS adjustment)

Equivalent vertical TEC at the pierce points
Assimilation effect

Background model

Cross section
19:33UT; -64.75ºE
from -40ºN to 10ºN

Analysis
GNSS TEC DA - Example 2

- For the assimilation
  - Calibrated (as in Themens et al. 2015) ground-based GNSS-derived slant TEC data from about 300 receivers located in the European region.

- For the validation
  - Manually scaled foF2 data obtained from Tromso (69.7ºN, 9.0ºE), Fairford (51.7ºN, 1.5ºW) and Juliusruh (54.6ºN, 13.4ºE) ionosondes at 1 hour time interval (only the result corresponding to Fairford will be illustrated).

- The data correspond the period 15-16 July 2017
Results: 15 July 2017; 14:00UT; FF051

vTEC at ionosonde longitude
- Background
- Analysis
- GNSS

Ne(h) at ionosonde location
- Background
- Analysis
- Ionosonde

Ne cross section at ionosonde longitude
Results: 16 July 2017; 14:00UT; FF051

**Background**

**Analysis**

Ne(h) at ionosonde location

vTEC at ionosonde longitude

Ne cross section at ionosonde longitude

**Background**

**Analysis**

Ne cross section at ionosonde longitude
Results: 15-16 July 2017 (sTEC DA)

foF2 time evolution at ionosonde location
Conclusions

• Specific examples have been presented to indicate that the NeQuick model can provide realistic “weather-like” descriptions of the 3-D electron density of the ionosphere, if suitable data ingestion and assimilation techniques are used.

• The ingestion techniques relying on the use of effective parameters allow NeQuick model to describe the storm-time space weather effects in terms of TEC.

• The analysis results have confirmed the effectiveness of the assimilation method based on the BLUE algorithm in reconstructing foF2, especially during geomagnetically disturbed conditions.
References


Thank you for your attention