

Using b-splines to Model Total Electron Content derived from Radio Occultation measurements by COSMIC satellites over the African region

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Outline

- ▶ Necessity for TEC modeling
- ▶ TEC from COSMIC radio occultation (RO) Data
- ▶ TEC Data organization
- ▶ The b-spline modeling technique
- ▶ Model validation using reserved RO TEC
- ▶ Model Validation using ionosonde TEC
- ▶ Conclusions

Necessity for TEC modeling

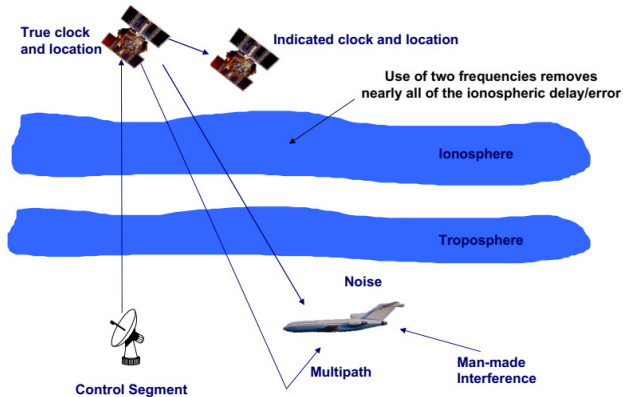


Figure: 1 (From MITRE presentation)

Examples of TEC models: NeQuick, International Reference Ionosphere, Klobuchar model

The COSMIC radio occultation (RO) TEC Data

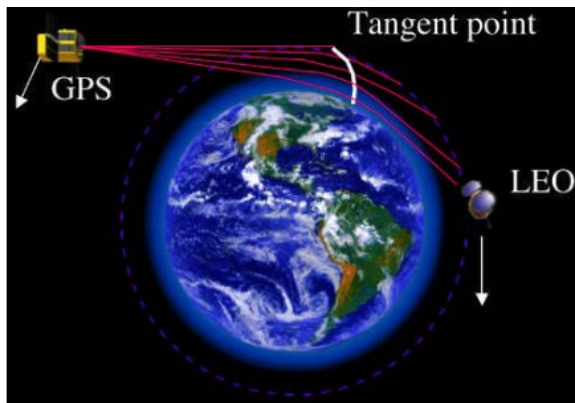
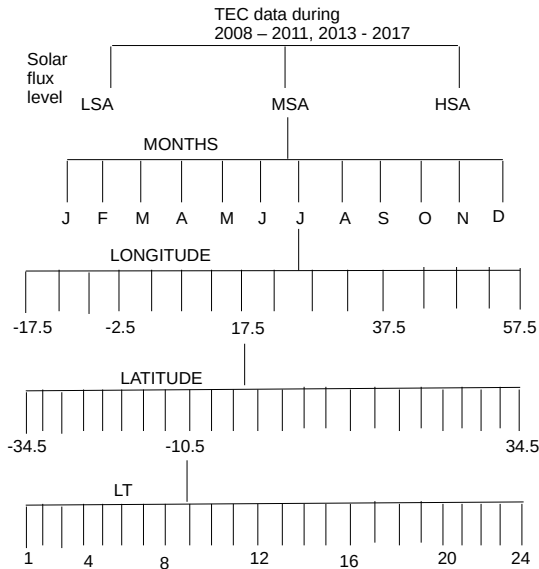


Figure: 2 (from Schreiner, et al. (1999). Analysis and Validation of GPS/MET Radio Occultation Data in the Ionosphere, radio sci.)

Inversion Techniques and Issues of filtering

TEC Data organisation (1/3)



TEC Data organisation (2/3)

- ▶ A total of 331,776 TEC data values were needed to exist in 16 longitudinal, 24 latitudinal, 3 solar flux, 12 monthly, and 24 hourly bins, in order to determine the model coefficients.
- ▶ However, from the data of the entire study period, only 121,447 bins were filled with TEC data values

TEC Data organisation (3/3)

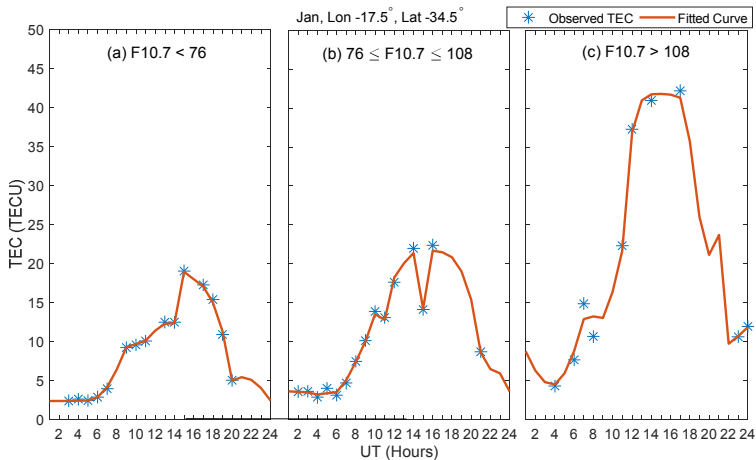


Figure: 3 Estimating Missing TEC values

B spline modeling technique

The TEC over African region was expressed as:

$$\text{TEC}(t, d, F, \lambda, \varphi) = \sum_{i=1}^{24} \sum_{j=1}^{12} \sum_{k=1}^3 \sum_{l=1}^{16} \sum_{m=1}^{24} a_{ijklm} N_i(t) \times \\ N_j(d) \times N_k(F) \times N_l(\lambda) \times N_m(\varphi)$$

De-Boor, C. (1978): A Practical Guide to Splines, Springer, New York, USA.

Model validation using reserved COSMIC RO TEC (1/2)

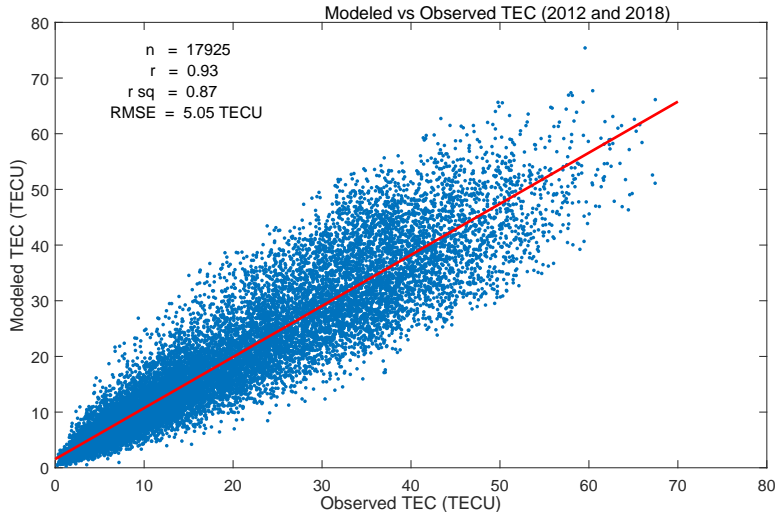


Figure: 4

Model validation using reserved COSMIC RO TEC (2/2)

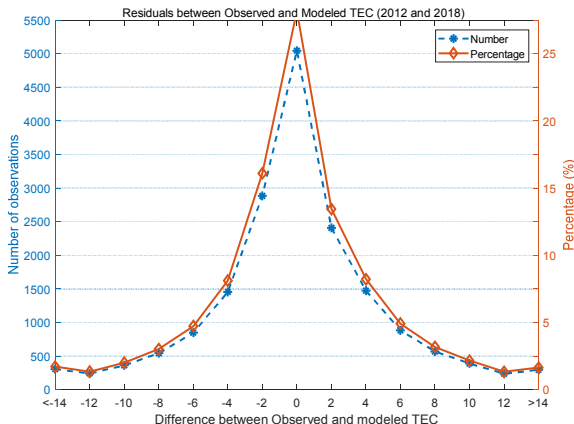


Figure: 5

Model validation using Ionosonde TEC (1/2)

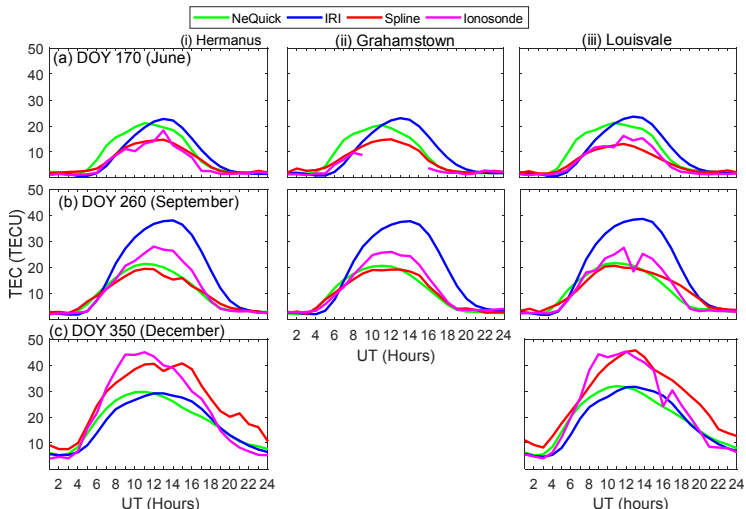


Figure: 6

Model validation using Ionosonde TEC (2/2)

r and RMSE associated with estimation of TEC observed at ionosonde stations by models (data for year 2013)

Ionosonde station (number of observations)	Model	r	RMSE (TECU)
Hermanus (n = 5110)	Spline	0.92	4.64
	IRI-2016	0.86	5.45
	NeQuick 2	0.92	4.10
Grahamstown (n = 4450)	Spline	0.88	5.56
	IRI-2016	0.82	6.29
	NeQuick 2	0.86	5.27
Louisville (n = 4543)	Spline	0.94	3.82
	IRI-2016	0.87	5.62
	NeQuick 2	0.94	3.73

Conclusions (1/2)

- ▶ TEC data obtained from RO by COSMIC satellites were binned according to local time, seasons, solar flux level and spatially.
- ▶ The coefficients of b-splines that were fitted to the binned data were determined by means of the least square procedure
- ▶ Validation exercise revealed that
 - (i) the observed and the modeled TEC correlate highly,
 - (ii) the modeled TEC closely approximates the observed TEC.

Conclusions (2/2)

- ▶ Validation of our model using TEC obtained from ionosonde stations yielded r values > 0.92 and RMSE < 5.56 TECU.
- ▶ The validation results imply that our model can estimate fairly well TEC that would be measured by ionosondes over locations which do not have the instrument.

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- (d) World data center at kyoto University, Japan (Kp and Dst)
- (e) NOAA (F10.7 flux and ionosonde measurements)
- (f) COSMIC data analysis and archive center

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Thanks for Listening