

**Cross Wavelet Analyses of Convection Electric field  
and  
Excess Equatorial Ionospheric TEC**

**Dr. Rajat Acharya  
Space Applications Centre, ISRO  
INDIA**

# Preamble

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- Space Weather affects the equatorial ionosphere
- One mean is through magnetosphere by generation of zonal electric field
  - Solar wind and IMF interact with the geomagnetic field*
  - During Southward direction of IMF Bz, magnetic reconnection occurs*
  - Convictional process starts. Charge separation generates electric field at poles*
- Electric field, readily gets transferred by Prompt Penetration.
  - Global-scale electric fields are not confined to high-latitude region.*
  - A correlated but short lived zonal field appears at the equatorial region*
  - Occurs when the counter field by R2 current temporarily out of balance*
- Zonal Electric field modulates the plasma drift and TEC
  - This zonal field, modulates the ExB drift of the ionospheric plasma.*
  - Effective recombination rate changes and hence in turn the TEC of the region varies.*

# Preamble

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- **Earlier works and motivation**

*Several models developed to relate equatorial electric field with IEF*

*Works by Kikuchi (1996), Huba et al. (2005), Manoj and Maus (2012), Wang et al., 2004; Hui Wang et al. (2008), Wiltberger et al. (2004) etc are popular*

*Few relate the IEF with the equatorial ionospheric TEC change occurring as a result*

- **This work**

*Challenging to identify effectiveness of this convectional electric field source towards variation in equatorial TEC. Work done towards this understanding*

*CWT is used on these two time series. CWT s better for feature extraction purposes. To examine how two time series are linked XCT and WTC used*

*Exposes regions of common power and phase in time-frequency explaining causality and effectiveness*

# Approach

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a. Inherent relationship is assumed

b. Convectional electric field used as one parameter.

*Derived from measured plasma velocity and magnetic field intensity, using the relation*  
 $E = -v \times B$

c. Excess TEC over the quiet day nominal values is also obtained

*Excess TEC over quiet day nominal values obtained by differencing corresponding VTECs*

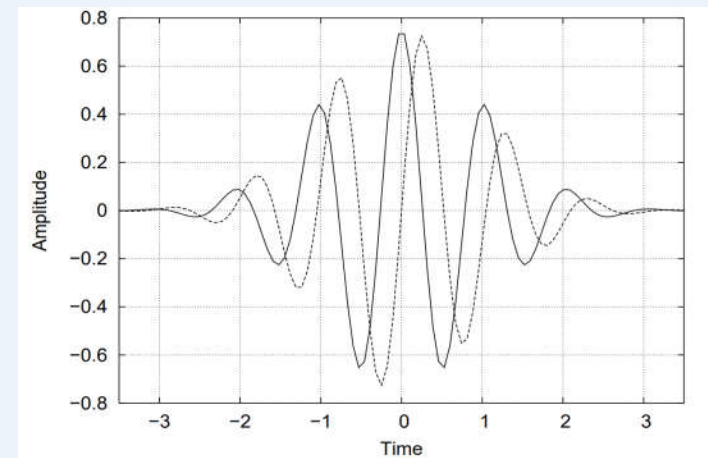
d. Wavelet analyses is done on both using Morlet's wavelet.

• *Function:*  $\Psi(\omega_0, \tau) = 1/\pi^{1/4} \exp(j\omega_0\tau) \exp(-\tau^2/2)$

• *CWT:*  $W_n^x(s) = \sqrt{(\delta t/s)} \sum_{k=1}^N x_k \Psi(k - n)$

e. Cross wavelet transform is obtained

f. Observations made and Conclusions derived out of it



# Data

## ■ Event

*St. Patrick's Day storm : 17–18 March 2015*

*2 CME on March, 15, 2015 and formed CIR in solar wind  
wind impinged upon magnetosphere at  $\sim 680$  km/s.*

*IMF Bz turned southwards  $\sim 0600$  hrs and  $\sim 1200$  hrs*

*Effective electric field of 200 mV/km was induced*

## ■ IEF obtained from online repository

*IEF data obtained from the OmniWeb portal of the GSFC. IEF  
data derived from B and the v values*

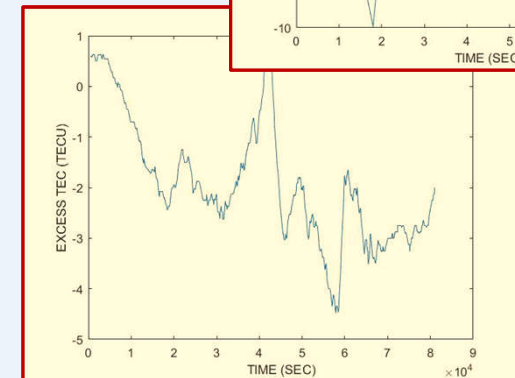
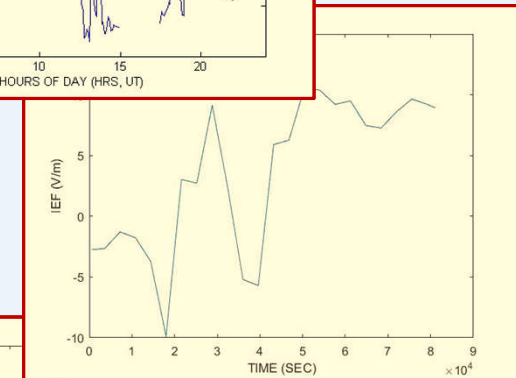
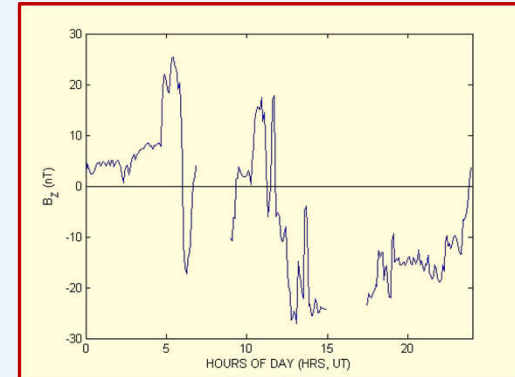
## ■ Excess TEC estimated

*TEC derived from GAGAN grid delay data at  $10^\circ\text{N}$ ,  $75^\circ\text{E}$*

*Excess TEC obtained as  $TEC_{event} - TEC_{quiet}$*

*$TEC_{quiet}$  data obtained by averaging TEC of two quiet days*

*Diurnal profile obtained is then used for the wavelet analysis.*

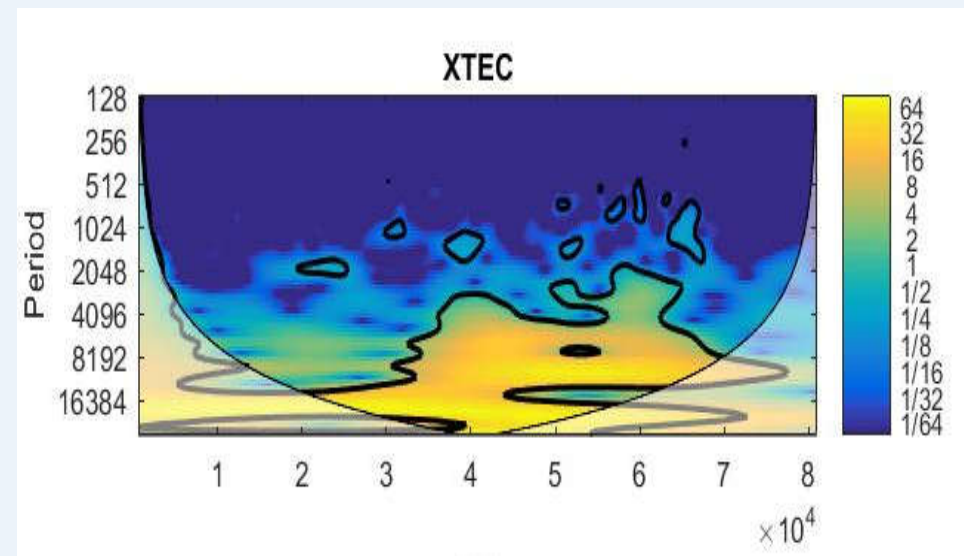


# Result

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## a. CWT coefficients of excess VTEC using Morlet wavelets.

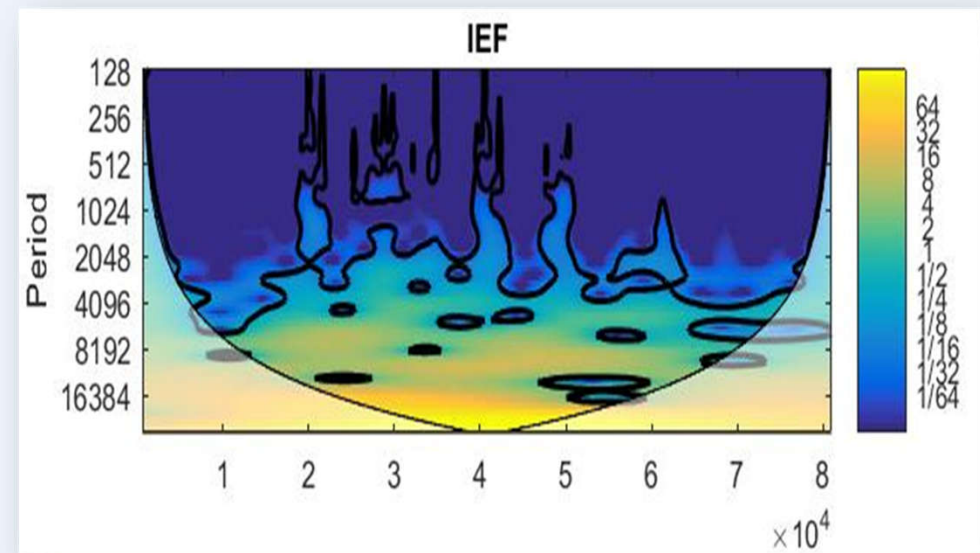
- *larger amplitudes at longer periods, particularly for periods > 2048 s*
- *Variations lesser than 30 minutes has negligible similarity with Morlet's wavelet*
- *Wavelet period 4096 – 8192 sec band showed high intensity after  $3 \times 10^4$  secs of day ( $\sim 10$  hrs) and continued till  $6 \times 10^4$  secs ( $\sim 18$  hrs) UT.*
- *For larger wavelengths, the maximum intensity remained near the noon*



# Result

## a. CWT coefficients of IEF using Morlet wavelets.

- Here too, larger amplitudes at longer periods, particularly for periods  $> 2048$  s
- Variations lesser than 30 minutes has negligible similarity with Morlet's wavelet
- Wavelet period 8192 – 16384 sec band showed high intensity after  $2 \times 10^4$  secs of day ( $\sim 06$  hrs) and continued till  $6 \times 10^4$  secs ( $\sim 18$  hrs) UT.
- For larger wavelengths, the maximum intensity remained near the noon



# Result

## a. The XWT results:

*Cross Wavelet Transform (XWT) identifies the areas of common power of two processes (without normalization) in time-frequency space*

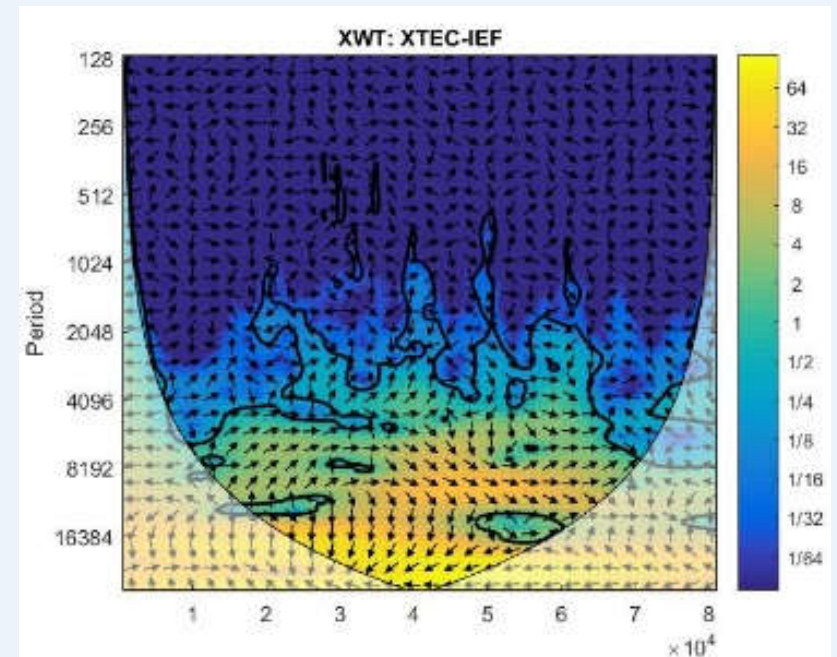
*Colour contour represents cross-wavelet power*

*Plot reveals large intensities are obtained for band of periods from 4096 and above around  $4 \times 10^4$  sec*

*Cross powers are not normalized and can imply artefacts. So, XWT is examined with phasors. Related phenomena show phase-locked XWT.*

*Phasor can be converted to time lag for specific period*

*Here, it is observed that different phase lag is obtained in different period bands*





# Result

## a. The WTC results:

*significant peak in the XWT might arise due to peak in one of the time series. To avoid such case, normalized WTC are calculated*

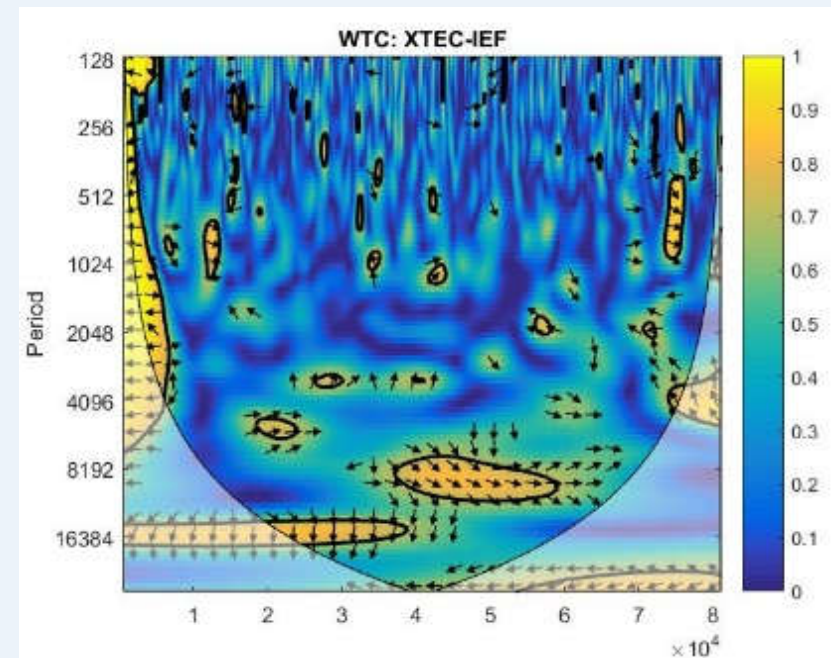
*Bounded Colour contour represents wavelet coherence*

*Detect strong cross-amplitudes of strength  $>0.9$  between the input electric field and the excess TEC which is in the 8192 sec period band.*

*Significant peaks around  $4 \times 10^4$  -  $5 \times 10^4$  sec*

*Compared to XWT, in WCT, most peaks vanish*

*The phasor angle  $\sim -45^\circ$  indicates a time lag of 1024 sec,  $\sim 17$  minutes*



# Conclusions

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The following conclusions can be drawn from the work

- a. The cross wavelet amplitude strength of  $>0.9$  re-establishes the causal relationship between the two variables in question
- b. Significant peaks appear around  $4 \times 10^4$  sec. implying that the maximum correlation can be observed only after the IEF is generated as a result of the under-shielding process
- c. The high WTC intensity for the wavelet period of 8162 corroborated to the earlier findings that the potential driving component has to be of period shorter than 8 hours.
- d. Uniform phase differences observed showed the phasor angle  $\sim -45^\circ$  which corresponds to a time lag of 1024 sec . This points towards a delayed manifestation of the effect of about 17 minutes.

Thank You

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