

United Nations / Philippines Workshop on the
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**PROBABILITY-OF-OCCURRENCE MODEL FOR GNSS
PNT UTILISATION RISK ASSESSMENT FACILITATES
GNSS APPLICATION DEVELOPMENTS IN THE
FIELDS OF AVIATION AND MARITIME**

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FACILITATES GNSS APPLICATION DEVELOPMENTS IN THE FIELDS OF AVIATION AND MARITIME
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- Content of presentation
- Introduction
- Hypothesis
- Material
- Method
- Concept/method demonstration
- Discussion
- Conclusion

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- Introduction
- Global Navigation Satellite System (GNSS) as a component of national infrastructure & application enabler
- GNSS PNT performance presented for ideal case of utilisation
- GNSS applications requires GNSS positioning performance description -> embedded in GNSS application Quality of Service (QoS)
- What is the risk of GNSS positioning performance failure in the provision of positioning performance (accuracy) required by GNSS application?

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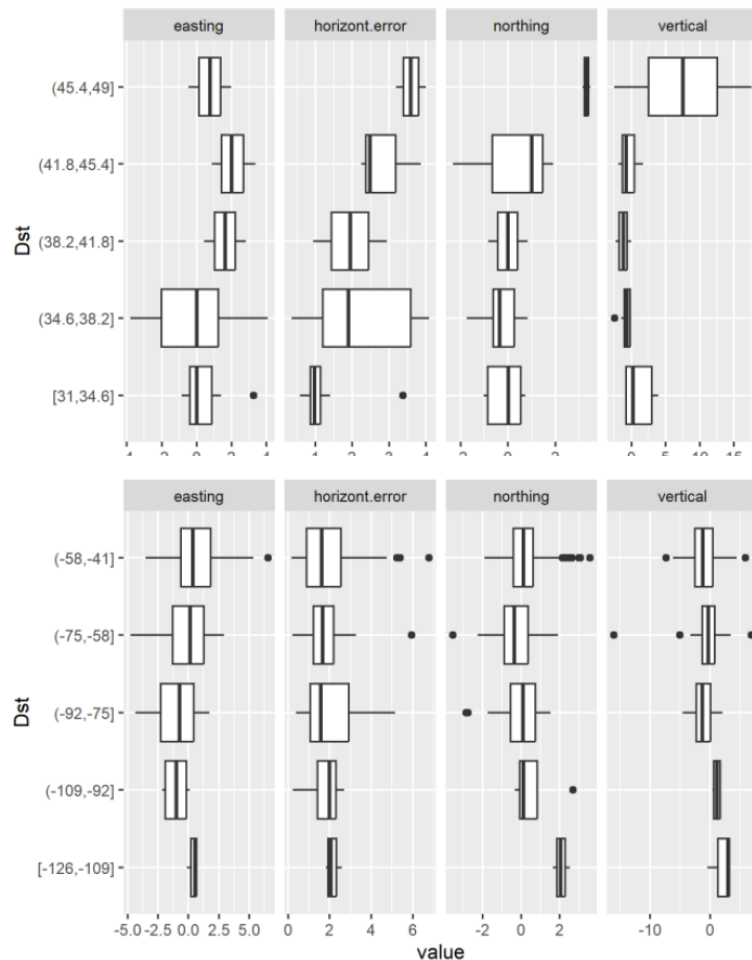
- Research hypothesis
- Sufficiently large dataset reflects the long-term statistical behaviour of GNSS positioning errors + proportional frequency of appearance of disturbing events -> a probabilistic model of the risk of GNSS positioning accuracy failure to meet the QoS requirements of a specific GNSS application

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- **Material (1/2)**
- The sufficiently large dataset is available that reflects the long-term statistical behaviour of GNSS positioning errors
-> continuous GNSS pseudorange observations at reference stations of International GNSS Service (IGS)
- This research utilises 365 days of GNSS pseudorange observations at Iqualuit, Canada
- The case of single-frequency GPS positioning errors, derived from GPS pseudorange observations, as observed in polar regions (Iqualuit)

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- Material (2/2)
- Statistical analysis of horizontal GPS positioning error of a commercial-grade single-frequency GPS receiver



GPS horizontal error [m]	No. of observations in 2014	Mean	Median	Variance
Total	1019769	1.9549	1.6300	4.89951
Dst > 30 nT	24	2.0077	1.5496	1.629124
Dst < -40 nT	222	1.8110	1.6709	1.328492

Compared with General	t-test, p-value, H0: means are equal	F-test, p-value, H0: variances are equal
Dst > 30 nT	0.8411	0.00227
Dst < -40 nT	0.06421	< 2.2e-16

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- Method (1/2)
- A single-function probabilistic model of the risk of GNSS positioning accuracy failure to meet the QoS requirements of a specific/targeted GNSS application -> **Probability of Occurrence (PoO) model**
- **GPS/GNSS Probability of Occurrence (PoO) risk index is defined based on empirical identification of the GPS/GNSS positioning degradation**

- Method (2/2)
- **Probability density function** $f_X(x)$ of statistical variable X

$$F_X(x) = P(X = x), F : \mathbb{R} \rightarrow [0, 1]$$

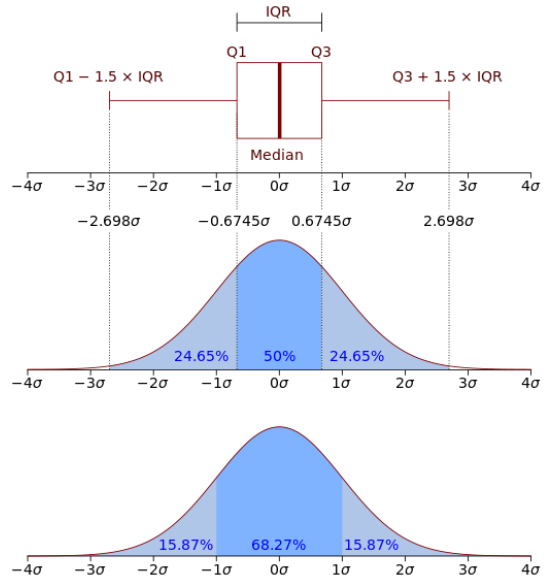
- **Cumulative distribution function** (CDF) $F_X(x)$ is defined as the function that returns the probability that X will acquire the value less than, or equal to x

$$F_X(x) = P(X \leq x), F : \mathbb{R} \rightarrow [0, 1] = \int_{-\infty}^x f_X(x) dx$$

- **Complementary cumulative distribution function** (CCDF), or tail distribution, is derived from the cumulative distribution function

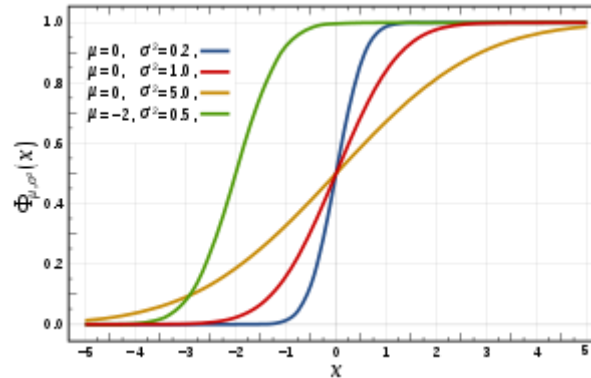
$$\bar{F}_X(x) = P(X > x) = 1 - F_X(x)$$

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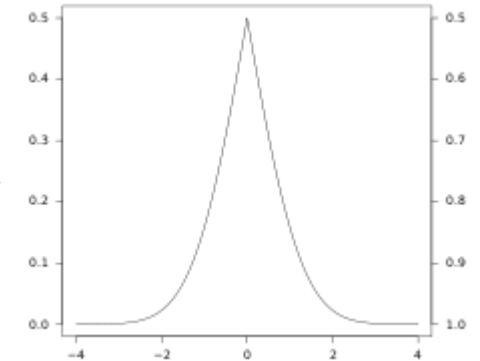
Source:
https://en.wikipedia.org/wiki/Probability_density_function

PDF



Source:
https://en.wikipedia.org/wiki/Cumulative_distribution_function

CDF



Source:
[https://en.wikipedia.org/wiki/Cumulative_distribution_function#Complementary_cumulative_distribution_function_\(tail_distribution\)](https://en.wikipedia.org/wiki/Cumulative_distribution_function#Complementary_cumulative_distribution_function_(tail_distribution))

CCDF

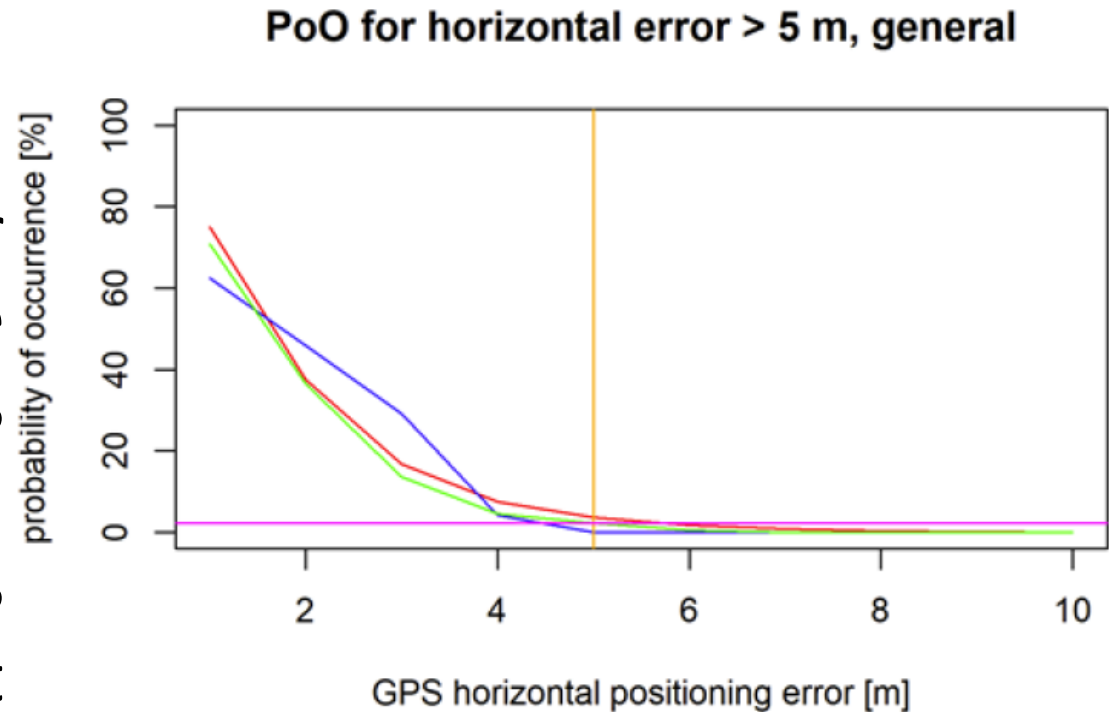
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- Concept/method demonstration
- Scenario: polar regions, single-frequency commercial-grade GPS receiver, GPS application with defined QoS
- PoO GPS risk model developed on GPS positioning error estimates derived from experimental GPS pseudorange observations in polar region in 2014

$$P_{risk} = f(\textit{requested horizontal accuracy})$$

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- Concept/method demonstration
- A specific GPS-based application should define its request for the highest acceptable horizontal GPS positioning error
- Example: GPS application requires that GPS positioning error should not exceed 5 m



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#EUSpace



Source: https://www.euspa.europa.eu/sites/default/files/report_on_maritime_user_needs_and_requirements.pdf

Table 88: Port authorities' interest in inte

Application	Horizontal accuracy in A 22/Res.915
Navigation in ports	1 metre
Tugs and pushers operations	1 metre
General port approaches	10 metres
Aids to navigation management	1 metre

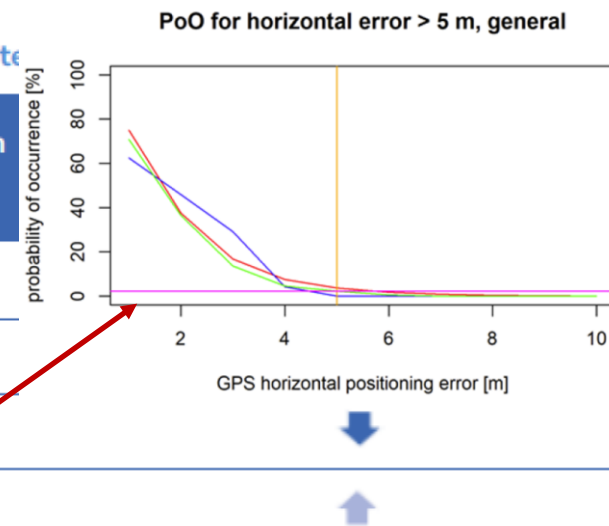


Table 90: e-GNSS performance requirements for autonomous vessels according to survey results.

Performance parameter	Oceanic deep-sea navigation	Coastal navigation
Horizontal accuracy 95%	<15m	<5m
Continuity (over 15 minutes)	$1 \cdot 10^{-5}$	$1 \cdot 10^{-6}$
AL	<28m	<12,5m
TTA	<8s	<6s
Integrity risk	$1 \cdot 10^{-6}$	$1 \cdot 10^{-7}$
Availability	99.8%	99.8%

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Typical operation	Accuracy horizontal 95% (Notes 1 and 3)	Accuracy vertical 95% (Notes 1 and 3)	Integrity	Time-to-alert	Continuity	Availability
En-route	3.7 km (2.0 NM)	N/A	$1 - 1 \times 10^{-7}/h$	5 min	$1 - 1 \times 10^{-4}/h$ to $1 - 1 \times 10^{-5}/h$	0.99 to 0.99999
En-route, Terminal	0.74 km (0.4 NM)	N/A	$1 - 1 \times 10^{-7}/h$	15 s	$1 - 1 \times 10^{-4}/h$ to $1 - 1 \times 10^{-5}/h$	0.99 to 0.99999
Initial approach, Intermediate approach, Non-precision approach (NPA), Departure	220 m (720 ft)	N/A	$1 - 1 \times 10^{-7}/h$	10 s	$1 - 1 \times 10^{-4}/h$ to $1 - 1 \times 10^{-5}/h$	0.99 to 0.99999
Approach operations with vertical guidance (APV-I)	16.0 m (52 ft)	20 m (66 ft)	$1 - 2 \times 10^{-7}$ In any approach	10 s	$1 - 8 \times 10^{-6}$ per 15 s	0.99 to 0.99999
Approach operations with vertical guidance (APV-II)	16.0 m (52 ft)	8.0 m (26 ft)	$1 - 2 \times 10^{-7}$ In any approach	6 s	$1 - 8 \times 10^{-6}$ per 15 s	0.99 to 0.99999
Category I precision approach (Note 7)	16.0 m (52 ft)	6.0 m to 4.0 m (20 ft to 13 ft) (Note 6)	$1 - 2 \times 10^{-7}$ In any approach	6 s	$1 - 8 \times 10^{-6}$ per 15 s	0.99 to 0.99999

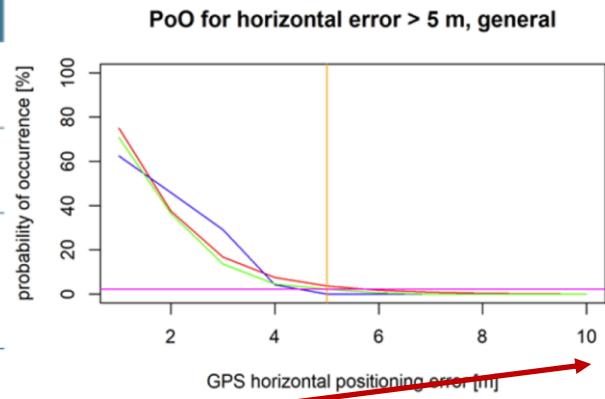


Figure 3: GNSS signal in space performance requirements – ICAO Annex 10 Vol I

Table 3: Nav equipment (GNSS receiver) performance requirements for Drone en-route PBN⁹

Operation	Hor (m) NSE(95%)	Ver (m) NSE(95%)	Integrity ¹⁰	TTA (s)	Alert limits (m)	Continuity	Availability
SAIL 3	3 - 8	4 - 13	$1 - 1E-4/h$	1 - 3	HAL: 25 - 27 (fixed wing) 10 - 14 (rotary) VAL: 12 - 22 (fixed wing) 7 - 23 (rotary)	$1 - 1E-4/h$	0.9999
SAIL 4	3 - 8	4 - 13	$1 - 1E-5/h$	1 - 3	HAL: 25 - 27 (fixed wing) 10 - 14 (rotary) VAL: 12 - 22 (fixed wing) 7 - 23 (rotary)	$1 - 1E-4/h$	0.9999

NOTE: The performance characteristics presented in this table are sufficient to deliver navigation performance equivalent to a RNP 26/16 m for fixed wing and RNP 12/14 m for rotorcraft due to improved FTE for rotorcraft

Source:
https://www.euspa.europa.eu/sites/default/files/report_on_aviation_and_drones_user_needs_and_requirements.pdf

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- Discussion
- The proposed method, and PoO model demonstrated in the proof-of-principle scenario, may be generalised towards any positioning indicator requested, as well as to utilisation multiple GNSS position estimation.
- GPS application operator and user may consider implementation and operation of a redundant positioning system in a confined area (port) to overcome the risk, or the utilisation of integrated navigation (for example, GPS+INS), for the period of degraded GPS positioning performance.

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- Conclusion
- This research proposes a single-function probabilistic model of the risk of GNSS positioning accuracy failure to meet the QoS requirements of a specific/targeted GNSS application -> Probability of Occurrence (PoO) model

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- Recommendations

- 1. Consideration of development & utilisation of a method of the Probability of Occurrence (PoO) model of GPS/GNSS application utilisation, especially in aviation and maritime.
- 2. Assemblage of a year-long massive databases of GPS positioning errors presented in the open-source access manner.
- 3. Fulfillment of, and support to, UN Sustainable Development Goals.
- 4. Facilitation of international collaboration of GNSS PNT performance observation collection and risk analysis in various conditions of use, applications, and influencing phenomena.
- 5. Utilisation of open source framework, such as R, for PoO model development and validation

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Baška, Krk Island, Croatia
16 – 18 June, 2024

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